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DYNAMIC RESPONSE ANALYSIS OF +G_x IMPACT ON MAN

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E. H. Root

NOVEMBER 1964

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FOREWORD

This study was conducted in support of Project 7231, Biomechanics of Aerospace, Task 723106, Biological Parameters of Impact. This task is assigned to the 6571st Aeromedical Research Laboratory, Holloman Air Force Base, New Mexico.

The computer program and the data reduction was supervised by Mr. F. P. Ehni, Chief of the Analog Computation Division, Air Force Missile Development Center, Holloman AFB.

This report was coordinated with the Biodynamics and Bionics Division of the 6570th Aeromedical Research Laboratories, Wright-Patterson AFB, Ohio. Following Dr. H. von Gierke's advice, particular emphasis was put on the Introduction (Section I) and the Recommendations (Section VI) to show how this study fits into the overall situation of impact research.

This technical report has been reviewed and is approved.

C. H. KRATOCHVIL
Major, USAF, MC
Commander

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ABSTRACT

An analog computer was used to compare the dynamic response of an accelerometer placed over the sternum of human test subjects during impact in $+G_x$ direction with the response of second and higher order spring-mass systems. Identity of the response modes of both systems, human and mechanical, was approximated by trial and error modification of natural frequency and damping coefficient of the computer model used. With restriction to only a few cases investigated and to the particular test conditions, best compliance of complete response coverage is considered to result from the application of a single spring-mass system of irregularly varying damping coefficient. A parametric analysis of the single spring-mass system is presented to aid the use of standardized impact profiles. The usefulness of the method of response approximation has been established, but the validation of the underlying concept of response predictability needs further investigation.

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LIST OF TABLES AND ILLUSTRATIONS

NOMENCLATURE

XYZ	Directional components
G	Acceleration factor in multiples of g ft/sec^2
$+G_x$	Acceleration factor in X direction applied to human subjects riding a sled in -X direction, backward facing position
a_i	Acceleration of sled (accelerometer in terms of $+G_x$)
$a_i(t)$	Time function of a_i
a_o	Acceleration of chest belt (accelerometer) in terms of G
$a_o(t)$	Time function of a_o
$\ddot{x}_i$	Acceleration input into spring-mass model in terms of G
$\ddot{x}_i(t)$	Time function of $\ddot{x}_i$
$\ddot{x}_o$	Acceleration output of spring-mass model in terms of G
$\ddot{x}_o(t)$	Time function of $\ddot{x}_o$
A_i	Peak acceleration of any impact profile, recorded, approximated or standard
A_o	First response peak recorded in $a_o(t)$
$A_o{}^*$	First response peak by approximation (feeding the recorded impact function $a_i(t)$ into the computer model
A_{o1}, A_{o2}, A_{o3}	First, second, third response peak of response function $\ddot{x}_o(t)$ of Standard Impact Profile $A_i(\sigma_1, \sigma_2, \tau)$
t_{A_o}, $t_{A_o}{}^*$, $t_{A_{o1}}$	Respective rise times of A_o, $A_o{}^*$, A_{o1}
$A_i(\sigma_1, \sigma_2, \tau)$	Standard Impact Profile (SIP), geometrically standardized shape of impact
τ	Total impact duration time of SIP
σ_1	Time factor in terms of τ of onset time of impact peak acceleration A_i of SIP
$\sigma_2 - \sigma_1$	Duration time of impact peak acceleration A_i in terms of τ

ω_n — Undamped natural frequency ($\sqrt{k/m}$) of SIP

ω_n^* — Undamped, natural frequency of human chest

$T = \frac{2\pi}{\omega}$ — Response established by trial and error approximation

ζ — Damping factor of SIP

ζ^* — Damping factor of human chest response established by trial and error approximation

ζ_i^* — Initial value of ζ^* before changes

INTRODUCTION

One reason for analyzing the effects of impact on man through treatment of the body as a dynamic mechanical system is founded in the hope of developing models which permit extrapolation from known test exposures of human subjects to injury criteria for untested acceleration environments. The overall approach underlying the development of such models is illustrated by the following diagram of the schematic breakdown of biodynamic response to impact.
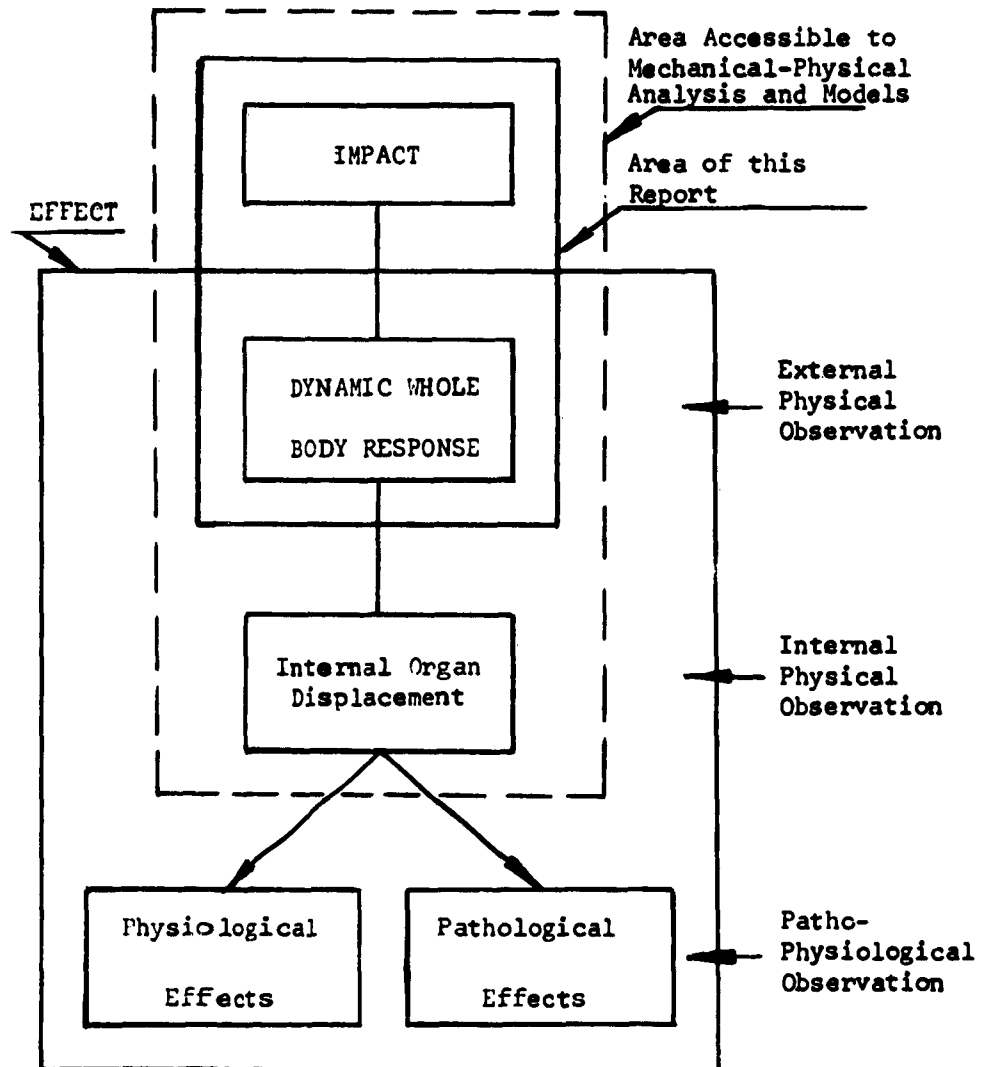
As shown, the impact environment acts on critical internal body structures to produce forces, organ displacements and deformations whose peak value and variation with time are a function of the dynamic response characteristics of the body in general, and of the particular structure and substructure, in particular. Any physiological or behavioral response to, or any pathological manifestation of impact is directly related to this dynamic response of the body or, more precisely, a result of relative displacement of one tissue structure with respect to another. The strain may produce either a disruption of structure resulting in frank injury or, short of mechanical fatigue or injury, the strain may induce alterations in the control mechanisms of the body which are manifest as changes in physiological parameters. The quantitation of pathophysiologic changes produced by high magnitude impacts usually requires examination of the specimen in detail and analysis of monitored physiologic data, which is not possible except in animal experiments. Cineradiographic techniques which are currently being refined are providing the possibility to begin studying the motions of internal organs, which will permit further quantitation of the dynamic response characteristics of segments of the body to impact.

Only through such detailed quantitative studies of the transmission of the mechanical energy from the environment to the point inside the body of final biological effectiveness, can one hope to achieve a more detailed quantitative understanding of the body's biological response as is presently available.

This paper deals with the first step in this direction by analyzing dynamic whole body response to impact. The data were obtained in connection with a large series of human tolerance tests on the Daisy Decelerator and were originally not primarily collected for this purpose. The dynamic response analyzed is the acceleration of the surface overlying the sternum of a seated subject exposed to $+G_x$ impact.

The method of analysis for the correlations between response and impact is in terms of the development of parameters for a spring-mass system with a similar excitation and response. The correlations are to be developed in terms of the characteristics of the impact such as peak value, onset rate, duration and offset rate and in terms of the characteristics of the equivalent spring-mass system such as resonant frequency and damping factor and variations of these parameters.

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THE BIODYNAMIC MODEL

The usefulness of the chosen biodynamic model is restricted to those body components directly or indirectly effected by or effective in the dynamic response of the thorax. Additional limitation accrues from the necessity due to the complex arrangements and properties of these body components to apply a model of analogy with reference to the involved body components as a lumped system rather than a model of true simulation.

The experimental conditions, described later, are illustrated by Figure 1.
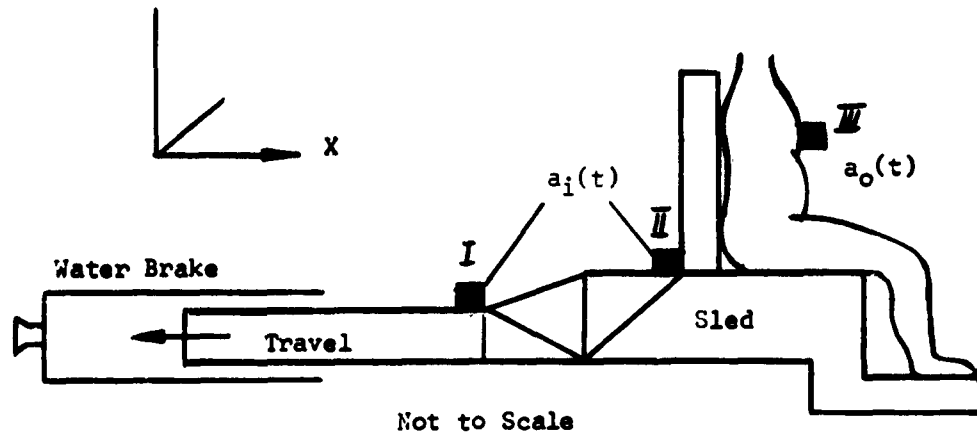
Figure 1   Impact Position

The human subject, seated on a sled, entered the water brake of the Daisy Decelerator in backward riding position (+G_x). The impact pulse $a_i(t)$ in X direction was measured by accelerometers placed on the piston (I) or the sled structure (II) behind the seat. The dynamic response $a_o(t)$ of the subject's chest was measured by accelerometers placed over the sternum (III) of the test subject clothed in a single layer surgical suit. The coordinates of measurements at location III (chest) are fixed with the accelerometer pad mounted on a chest belt applied over the suit. The sled/body mass ratio was about 10:1.

a. Physical Model (Figure 2)

Since accelerometer measurements always refer to the earthbound coordinate system it was desired that the chosen derivation of the differential equation concurs with the applied instrumentation.
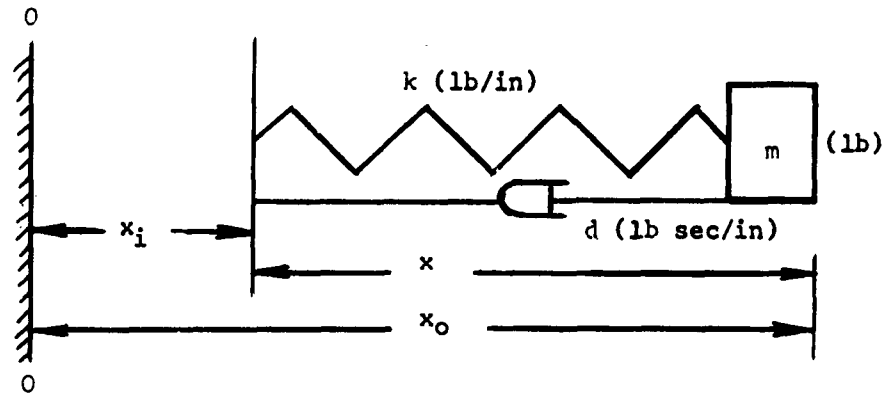
Figure 2 Physical Spring-Mass System

With line 0-0 as earth fixed reference, the differential equation of the assumed spring-mass system is written in the form:

$$\ddot{x}_o + \frac{d}{m}\dot{x} = \frac{k}{m} x = 0 \tag{1}$$

$\ddot{x}_o$ is the acceleration of the assumed mass m to be compared with the (output) measurement a_o of the chest accelerometer at location III (Fig. 1). The displacement x_o of the mass m is thought to be not identical with the elongation x of the assumed spring. Since the spring mass system is used as a model of analogy, the mass m (lb),

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the damping factor d (lb sec/in), and the spring constant k (lb/in) of
this physical model do not have any known relation to the physical
properties of the body (components). It is the purpose of this study
to investigate whether or not the dynamic response characteristics of
the human trunk exposed to $+G_x$ impact can be simulated by a simple
spring-mass system in terms of undamped natural frequency $\omega_n(=\sqrt{k/m})$
and dimensionless damping coefficient $\zeta(= 1/2\ d/\ \sqrt{mk})$.

By use of

$$x = x_o - x_i \; ; \; \dot{x} = \dot{x}_o - \dot{x}_i$$

and the substitutes

$$k/m = \omega_n{}^2 \text{ and } d/m = 2\zeta\omega_n$$

equation (1) is transformed into

$$\ddot{x}_o + 2\zeta\omega_n\dot{x}_o + \omega_n{}^2 x_o = 2\zeta\omega_n\dot{x}_i + \omega_n{}^2 x_i \qquad (2)$$

In Laplace notation, equation (2) can be written as the transfer function

$$\frac{x_o(s)}{x_i(s)} = \frac{2\zeta\omega_n s + \omega_n{}^2}{s^2 + 2\zeta\omega_n s + \omega_n{}^2} \qquad (3)$$

where s is the commonly used Laplace Operator.

Multiply both sides of the equation with s^2 it is

$$\frac{x_o(s)s^2}{x_i(s)s^2} = \frac{\ddot{x}_o}{\ddot{x}_i}$$

Where $\ddot{x}_i$ and $\ddot{x}_o$ can be compared with the acceleration a_i and a_o
measured at location I (or II) and III respectively (Fig. 1).

On the analog computer, equation (3) was mechanized with ω_n and ζ
as adjustable variables (Fig. 3). A time expansion of 100 was used
for convenience.

b. <u>Mathematical Model Modification</u>

The second order system (equation 3) can be enlarged to the
fourth or sixth order by writing

$$\frac{a_1 s + b_1}{(s^2 + a_1 s + b_1)(s^2 + a_2 s + b_2)}$$

Figure 3   Analog Computer Block Diagram

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respectively

$$\frac{\alpha_1 s + b_1}{(s^2 + \alpha_1 s + b_1)(s^2 + \alpha_2 s + b_2)(s^2 + \alpha_3 s + b_3)}$$

identified by the factors

$$\omega_{n_1}, \omega_{n_2}, \omega_{n_3}, \quad \zeta_1, \quad \zeta_2, \text{ and } \zeta_3.$$

This modification cannot be identified with a set of coupled spring-mass systems unless one would neglect the reaction of the second system to the first and so forth. However, the mathematical model modification can be used for qualitative comparison between second order and higher order systems.

III

EXPERIMENTAL PROCEDURES

a. <u>Human Testing</u>

The human impact tests under consideration were not designed to satisfy the technical aspects of this study but were governed by the objectives of typical go-no-go testing; i.e., in each case the test subject was observed by physical examination as to his hematological responses as the reaction to a particular impact pulse applied to the test sled.

In application to this study, it was hoped that test subjects having had more than one run might offer a better chance of a recognition of trends. On this basis only the tests of Table I were selected from available series of backward-facing (+G_x) impact.

The tests used comprise a number of instrumentational changes. No recordings of physiological data were made prior to test No. 359. Only the acceleration-time histories of the sled, $a_i(t)$, and of the human chest $a_o(t)$, were recorded. Two accelerometers, both measuring in X direction were mounted on the sled piston (location I). Two accelerometers placed over the sternum (location III) of the test subject also were oriented in X direction; however, tilting of the chest accelerometers, i.e., the position of their coordinates, was not controlled during impact.

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Table I Selection of Human Tests

Test No.	Test No.	Subject Name	Height (in)	Weight (lbs)	Sled (A_i) Peak "G"	Chest (A_o) Peak "G"	Test Variation
318				135	25/26	66/43	The "# 300"
335	I	ELB	70	135	40	86/78	series mea-
589				140	14	21.5	surements
							are less
							reliable than
319				155	25.5	38	all other
612	II	JDM	70	171	15	23.5	subsequent
842				169	20	31	tests for
							which a more
							stable accel-
320				170	23.5	43	erometer
607	III	RAG	69	175	14	25	mounting was
755				172	20.5	29.5	used.
332				118	36.5	54	
592	IV	AVZ	65	120	15	22	
606				150	16	27.5	
790	V	RH	67	155	10.5	18	*
751				155	19	22	
846	VI	MCS	68	160	19	33	
798				154	23.5	27	*
756				145	21.5	27.5	
844	VII	CHSW	67	150	20	29	

* In these tests a 24-pound parachute (including harness) was placed over the chest of the test subject and the response accelerometer was placed over the chest parachute.

With test No. 359, a change of the chest and sled instrumentation was introduced. At both locations I and III, three accelerometers, recording in three coordinates X, Y, and Z, were applied. Only the recordings in X direction were used in this analysis. A double chest strap was used to accommodate the chest accelerometers, with coordinate positions still uncontrolled during impact. Test No. 390 and all consecutive tests included ECG recording. Starting with test No. 592, the three sled accelerometers were removed from the sled piston (location I) and mounted at the sled structure closer to the seat (location II).

Tests No. 300 through 335 are reported in a previous publication[1].

b. Response Approximation

The records of the impact acceleration $a_i(t)$ measured at location I (or II) were used as the input function $\ddot{x}_i(t)$ of the computer and were transformed by a curve follower into volts as a function of time. The output function $\ddot{x}_o(t)$ of the computer was plotted by an x-y plotter on translucent paper overlaying the pre-drawn, actually recorded chest acceleration $a_o(t)$ measured at the sternum of the test subject (location III). Potentiometers for $\omega_n{}^*$ and ζ^* were controlled manually in successive computer runs until a close fit between computer output $\ddot{x}_o(t)$ and recorded chest response $a_o(t)$ was achieved.

1. Complete Response Coverage

The physical model second order (Section IIa) and its mathematical modification to a model of higher order up to the sixth (Section IIb) were used to determine the significance of the choice variables. Tests No. 319, 612 and 842 are discussed as typical examples:

Test No. 319 (Fig. 4). A second-order system of constant $\omega_n{}^* = 163$ rad/sec and constant damping coefficient $\zeta^* = 0.65$ failed to approach the acceleration-time history of the record. By use of two second-order systems ($\omega_{n1}{}^* = 163$, $\omega_{n2}{}^* = 194$) satisfactory compliance of the complete response mode could be obtained but only with the damping coefficient $\zeta_2{}^*$ varying from 0.03 to 0.9 after a time of 0.0625 second, with a constant setting of $\zeta_1{}^* = 0.65$.

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[1] Beeding, Eli L., and John D. Mosely. Human Deceleration Tests. AFMDC-TN-60-2, Holloman AFB, New Mexico, January 1960.
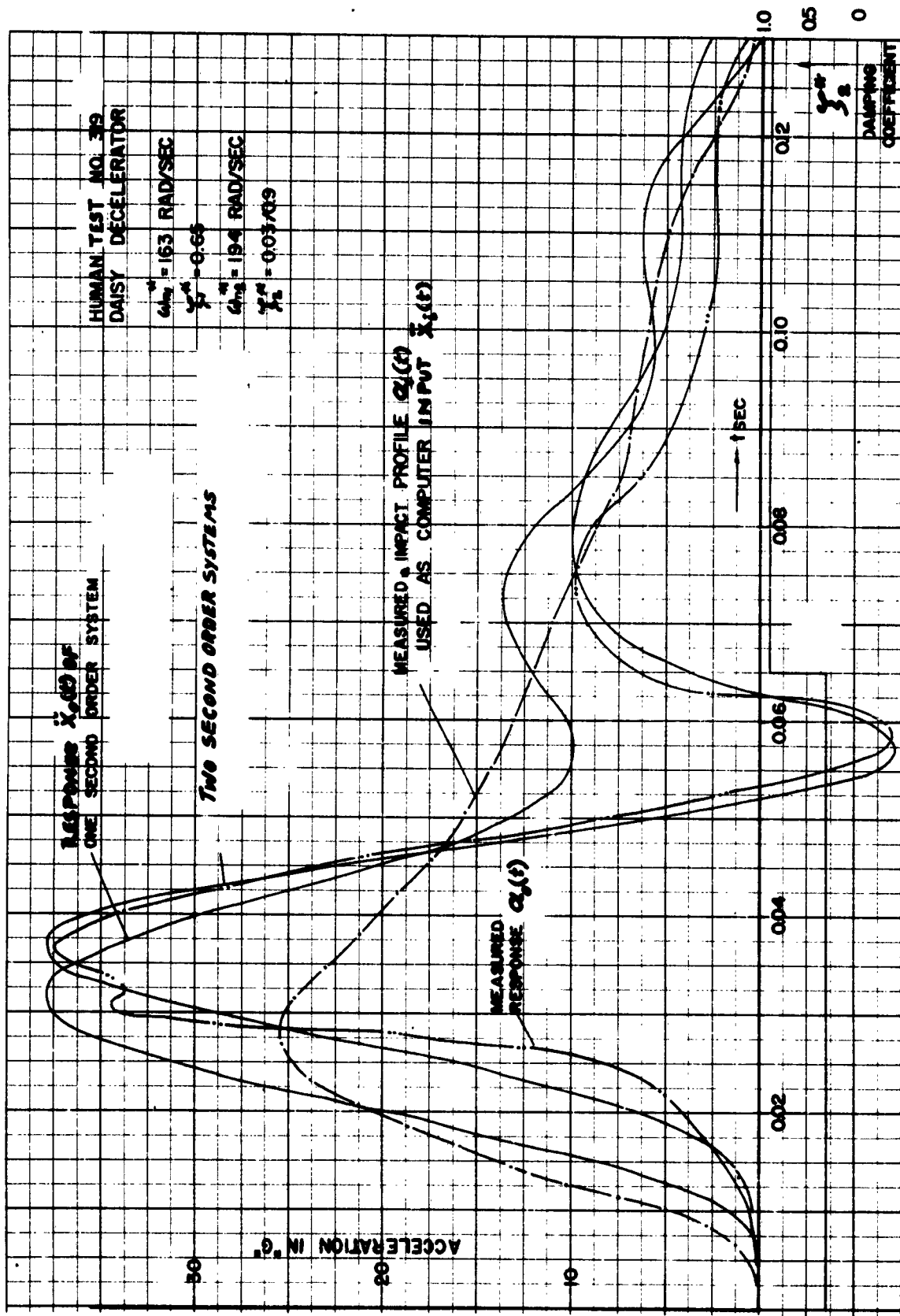
Figure 4   Complete Response Coverage of Human Test No. 319

Test No. 612 (Fig. 5). Compliance was considered satisfactory for constant $\omega_n^* = 145$ rad/sec and a change of the damping coefficient from 0.25 to 0.75 at the time of 0.045 second.

Test No. 842 (Fig. 6). Comparison is made for a second-order system between two approaches, one of constant ω_n^* and constant ζ^*, the other of constant ζ^* and continuously varying ω_n^*. In this test, response peak and onset time were approximated somewhat better by varying ω_n^*.

2. Limited Response Coverage

All tests were rerun on the computer with the requirement to establish best compliance of first response peak and its onset time by use of the second order, physical model (Section IIa) for constant ω_n^* (per run) and constant damping coefficient ζ^* (per run). The results are illustrated in Figures 7 through 13. Natural frequency ω_n^* and damping ζ^* are considered as criteria of comparison between runs of same and different test subjects.

Test No. 318 and 335, Figure 7, illustrate a very erratic onset of the input peaks of 26G and 40G respectively, recorded at location I of the sled (Fig. 1). Test No. 319, Figure 8, shows a very unrealistic double peak of the dynamic chest response $a_o(t)$. For both tests the highest response peak A_o recorded by accelerometer No. a of 66G and 86G could not be simulated by the computer for any value of ω_n^*. The differences of response peaks of same test No. 318 recorded by accelerometers Nos. a and b could not be explained as to their cause. Therefore, the response data of the "No. 300" test series cannot be used for comparison.

Tests No. 790 and 798, Figures 11 and 12 respectively, differ from all other tests by the use of a 24-pound chest parachute to which the accelerometer pad was attached for otherwise unchanged test conditions. Here, too, a comparison with other tests might be misleading.

All other plottings of Figures 7 through 13 are self-explanatory. In each case the electronic recording system filtered out all vibration frequencies beyond 300 c.p.s. of the sled impact pulse measured at location I or II. The recording of the chest response dynamics (location III) was usually not superimposed by noise.

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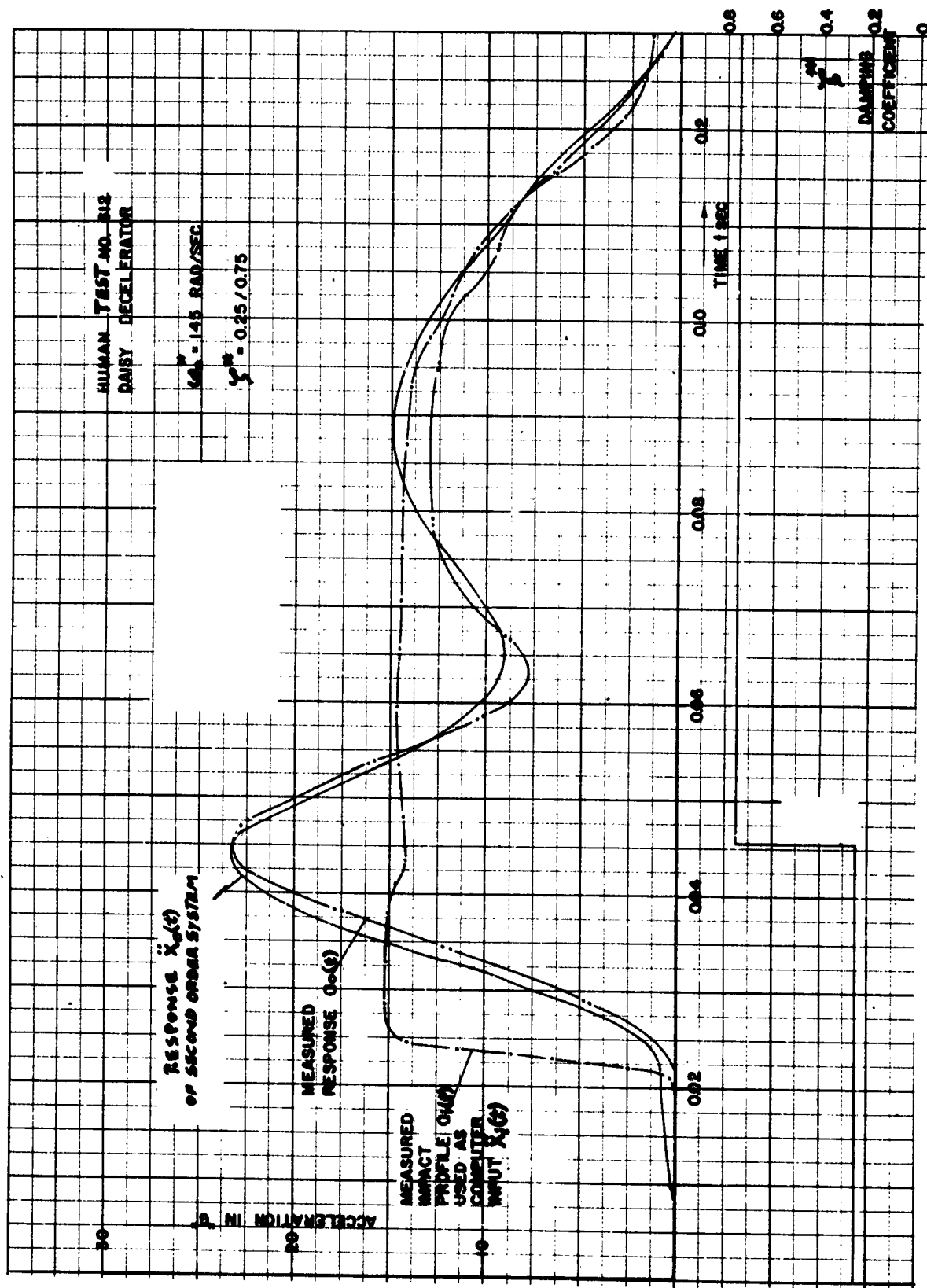
Figure 5   Complete Response Coverage of Human Test No. 612

12
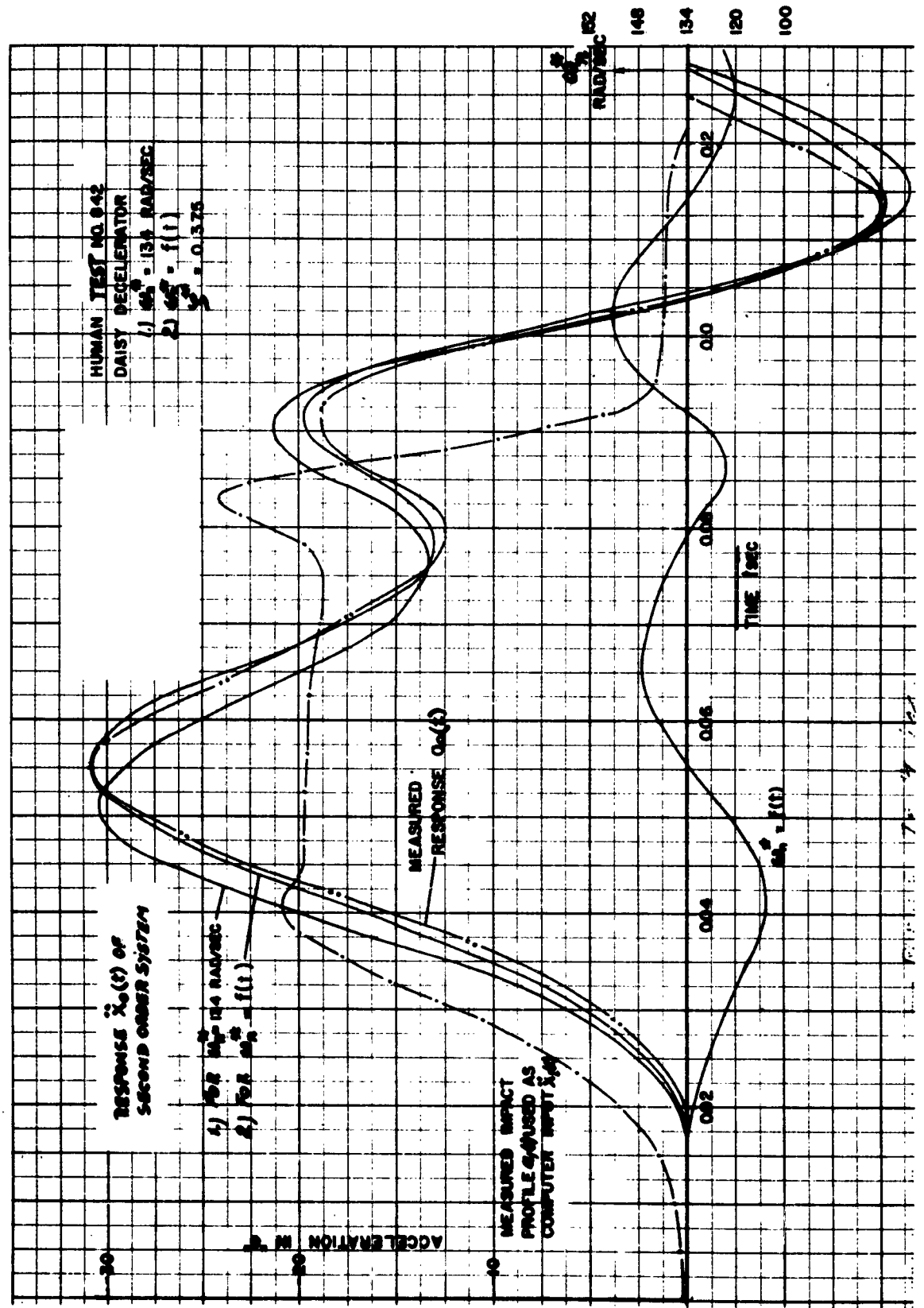
Figure 6   Complete Response Coverage of Human Test No. 842

13
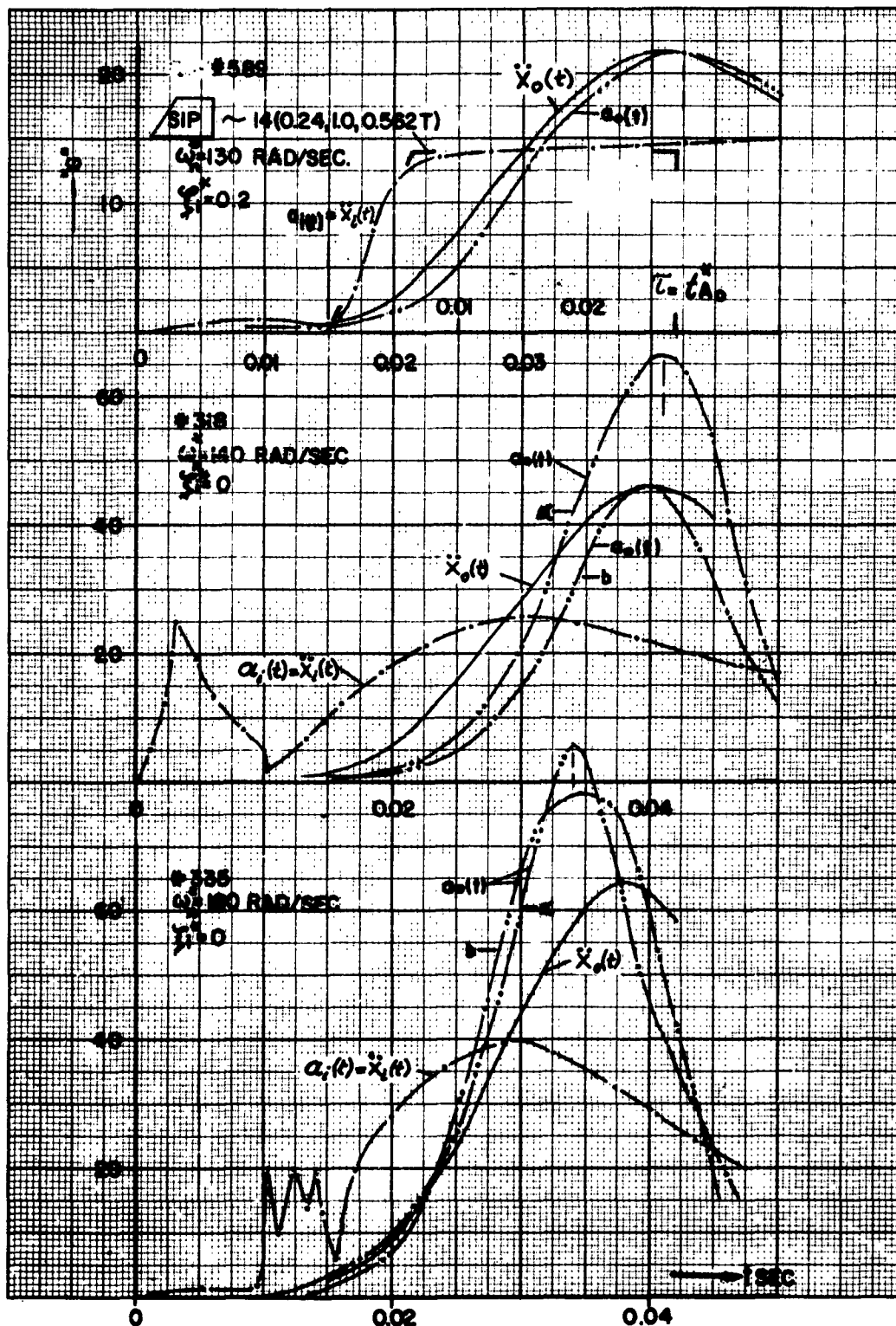
Figure 7   Limited Response Coverage (First Response Peak)
Tests No. 589, 318 and 335.

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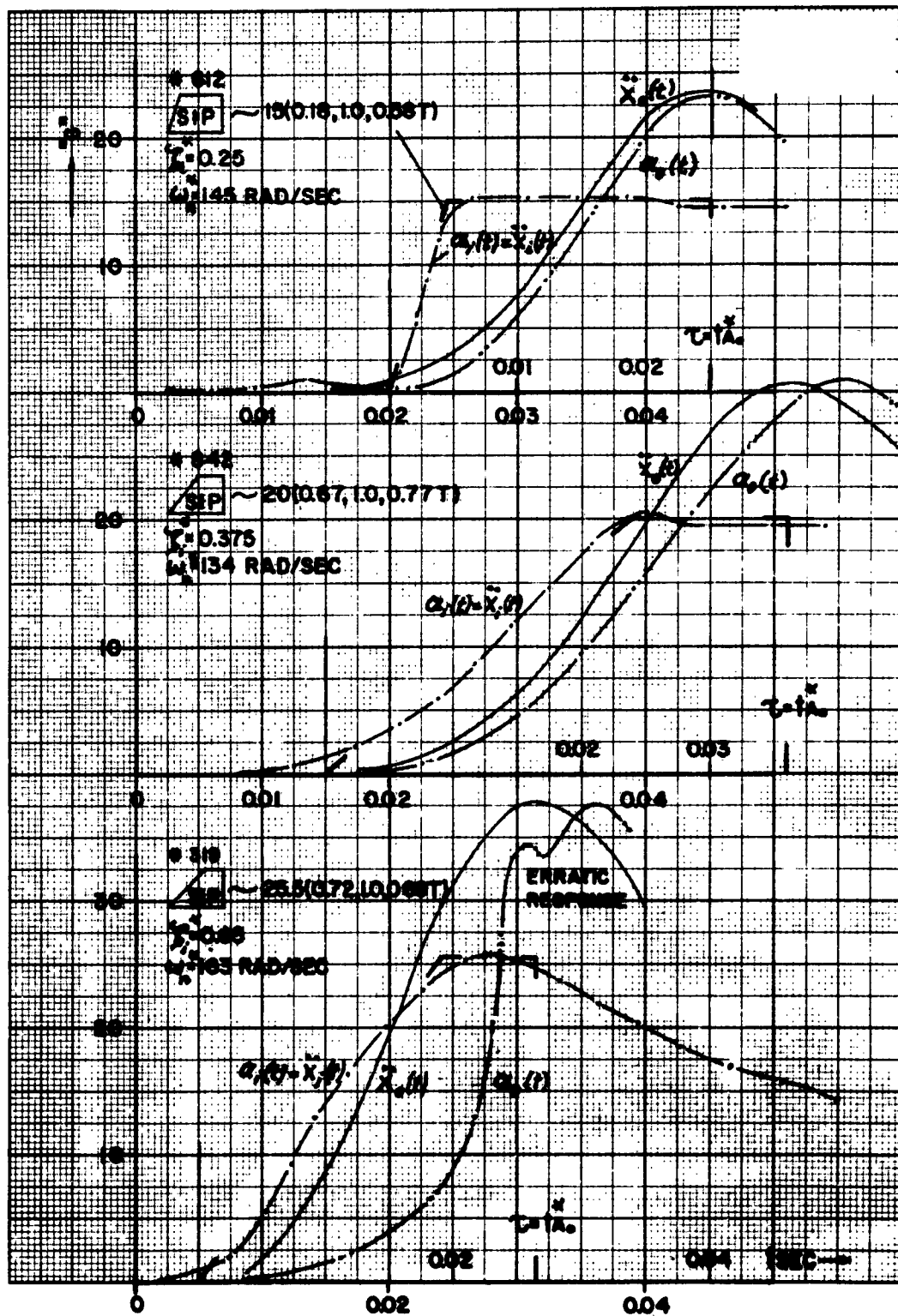
Figure 8   Limited Response Coverage (First Response Peak)
Tests No. 612, 842 and 319.

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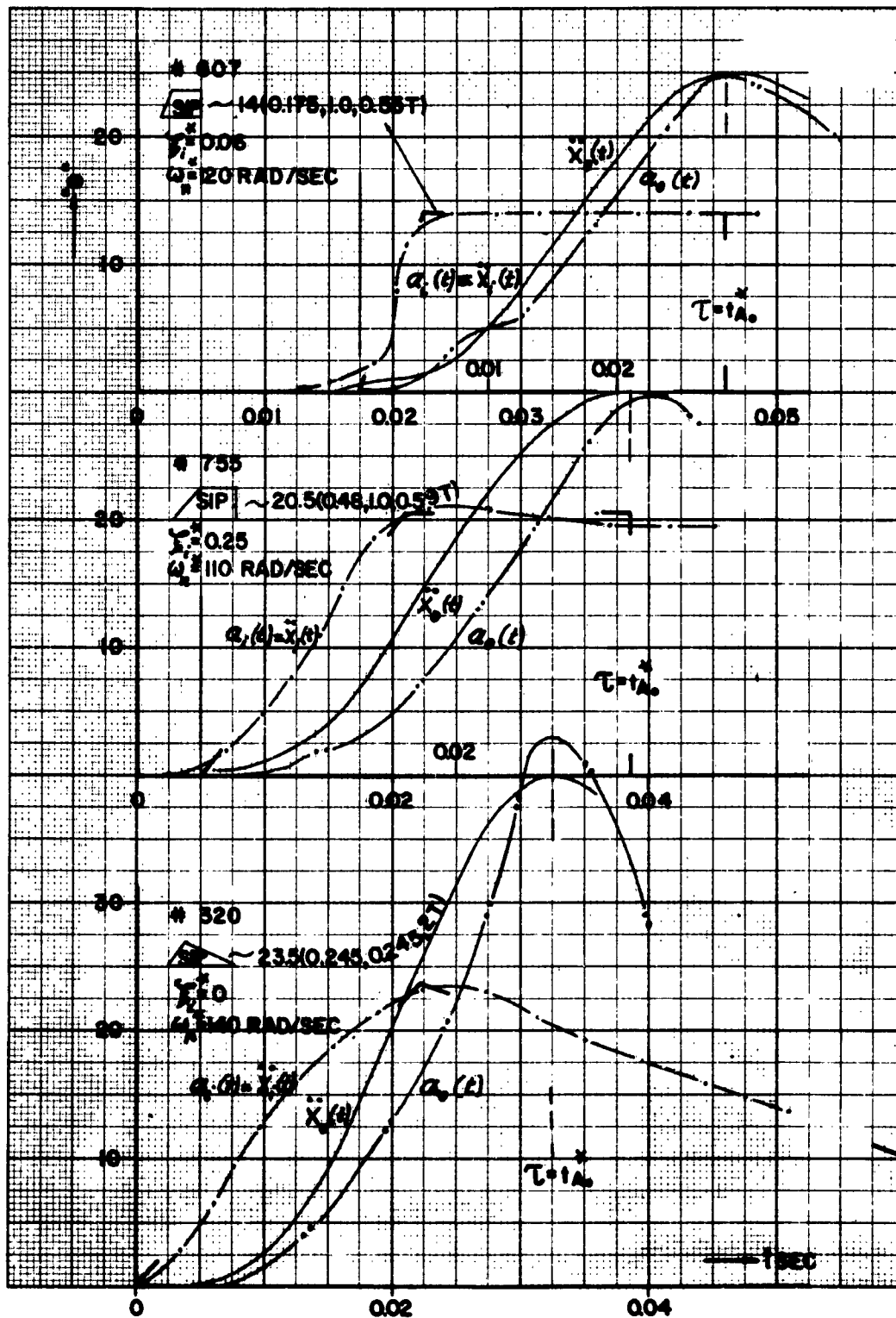
Figure 9   Limited Response Coverage (First Response Peak)
Tests No. 607, 755 and 320.

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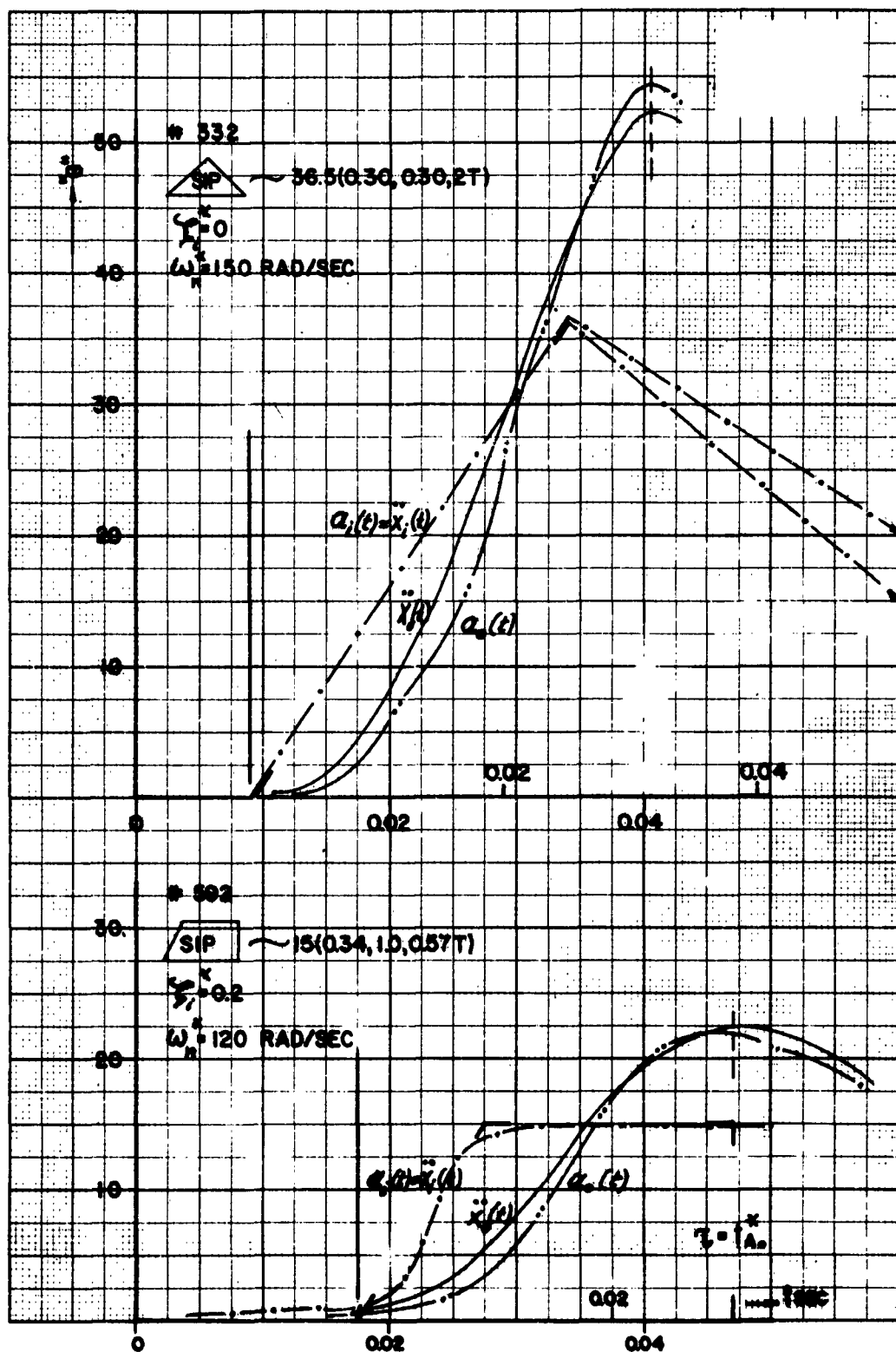
Figure 10 Limited Response Coverage (First Response Peak)
Tests No. 332 and 592.
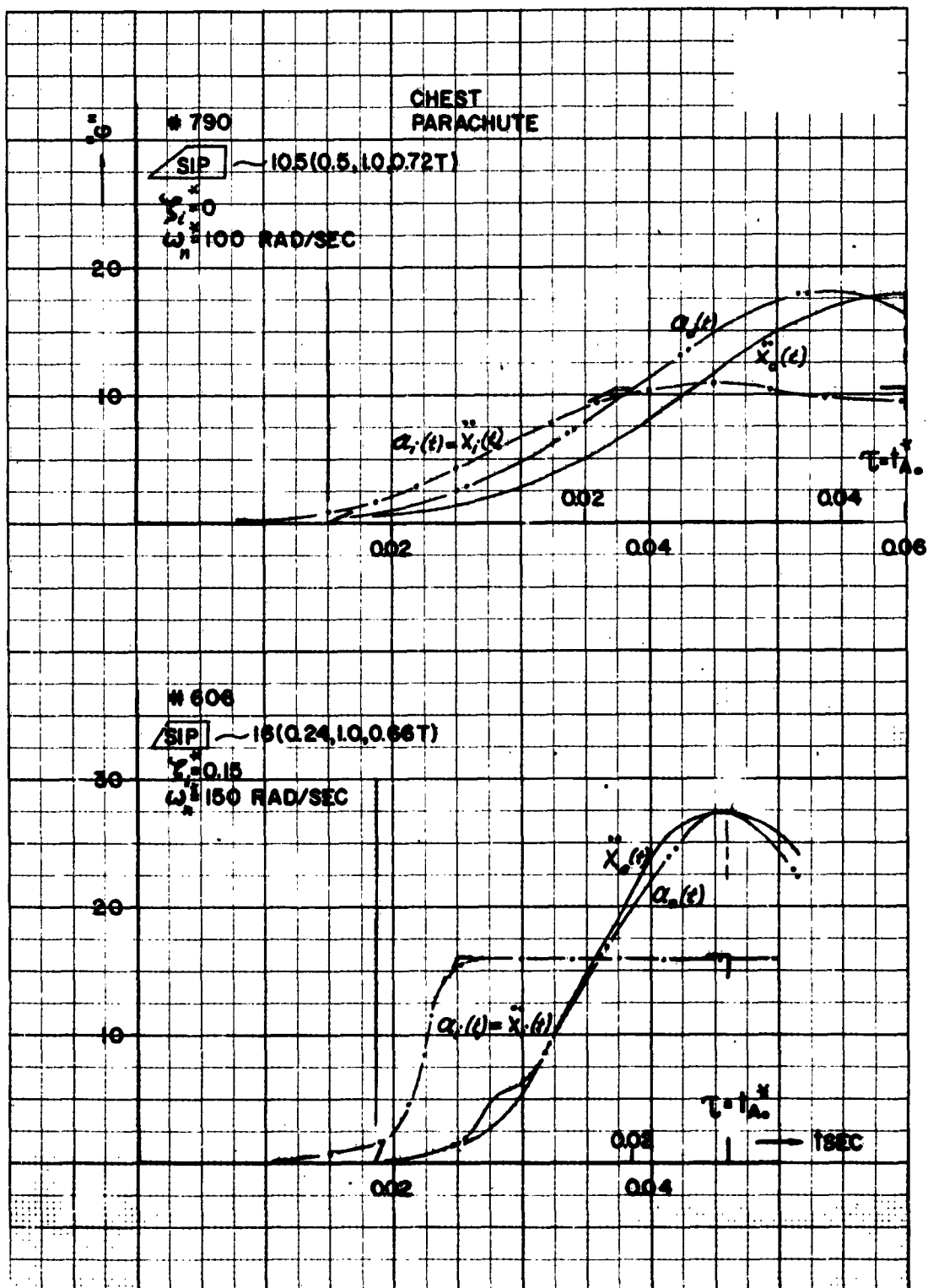
Figure 11   Limited Response Coverage (First Response Peak)
Tests No. 790 and 606.

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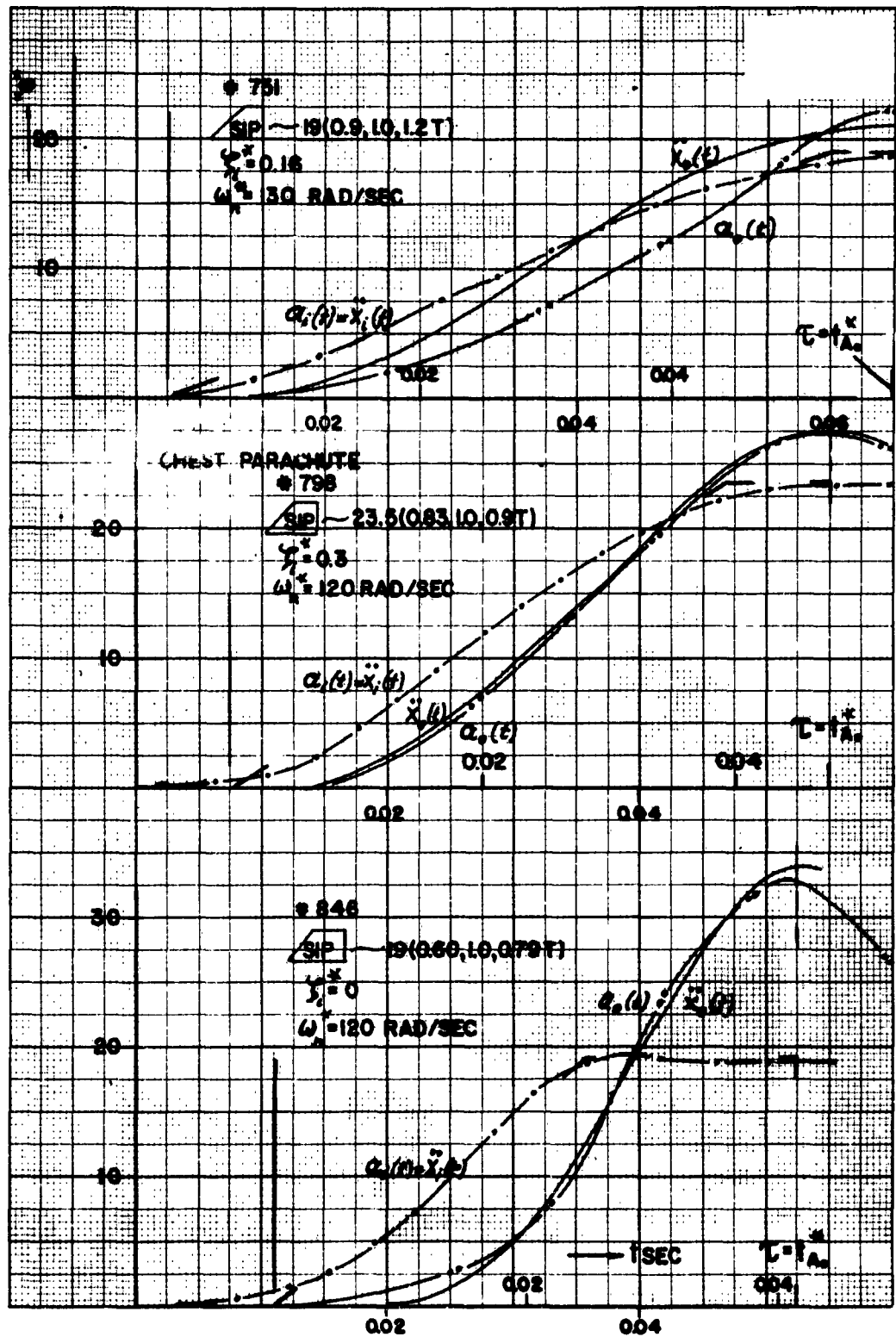
Figure 12   Limited Response Coverage (First Response Peak)
Tests No. 751, 798 and 846.
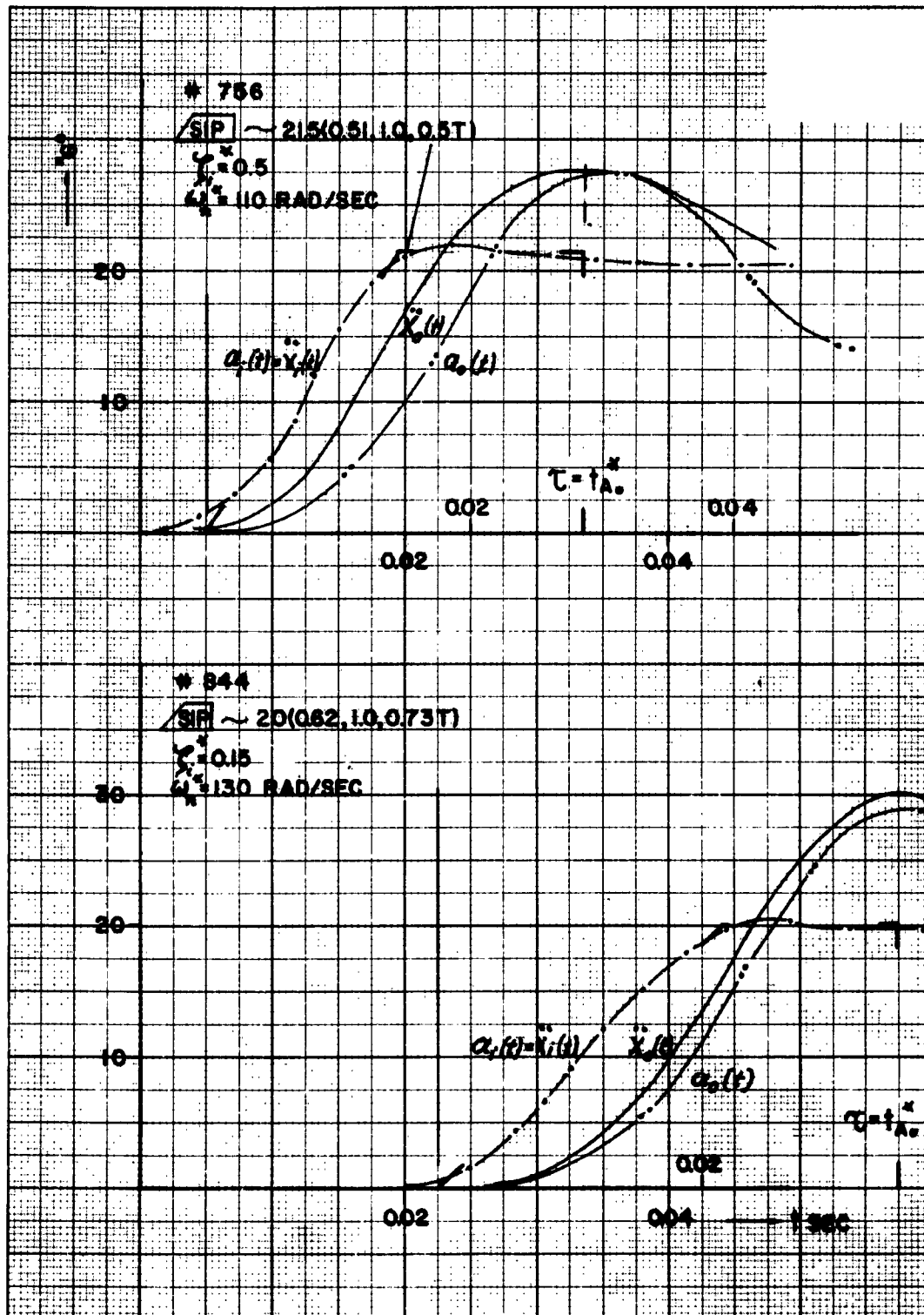
Figure 13   Limited Response Coverage (First Response Peak)
Tests No. 756 and 844.

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The recorded impact profiles $a_i(t)$ as measured at sled locations I or II were "hand smoothed" (Section IVb) before being applied as the input profile $\ddot{x}_i(t)$ of the computer model. In addition, the "hand smoothed" impact profiles were replaced by standardized impact profiles in an attempt to generalize the test evaluation as outlined in the following section.

c. Standard Impact Profile (SIP)
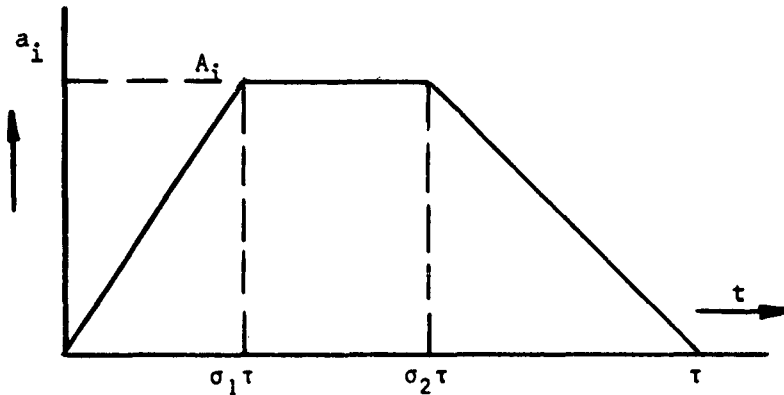
Figure 14 Standard Impact Profile

The Standard Impact Profile (SIP) can be termed symbolically as SIP $\sim A_i$ (σ_1, σ_2, τ) where A_i is the peak acceleration, τ the impact duration, σ_1 the time factor of peak onset, and $\sigma_2 - \sigma_1$ the time factor of peak duration with reference to τ.

The impact parameters for this profile are given in explicit form[2] for accelerated motion,

$$D = \frac{\sigma_1^2 - \sigma_2^2 - 3\sigma_1 + 2\sigma_2 + 2}{3(1 + \sigma_2 - \sigma_1)} \cdot v_f \tau \quad ; \quad A_i = \frac{2}{1 + \sigma_2 - \sigma_1} \cdot \frac{v_f}{\tau}$$

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[2] Feder, H.C. Nomographs for Multiphase Acceleration Profiles. AFMDC-TR-60-9, Holloman AFB, New Mexico, June 1960.

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for decelerated motion,

$$D = \frac{\sigma_2{}^2 - \sigma_1{}^2 + \sigma_2 + 1}{3(1 + \sigma_2 - \sigma_1)} \cdot v_i\tau \;\; ; \;\; A_i = \frac{2}{1 + \sigma_2 - \sigma_1} \cdot \frac{v_i}{\tau}$$

(D = travel distance, v_f = final velocity of acceleration, initial velocity zero, v_i = initial velocity of deceleration, final velocity zero.) These equations are useful for test programming and evaluation in regard to A_i, D, v, and τ for variable values of σ_1 and σ_2.

1. **Standardization of Impact Profile**
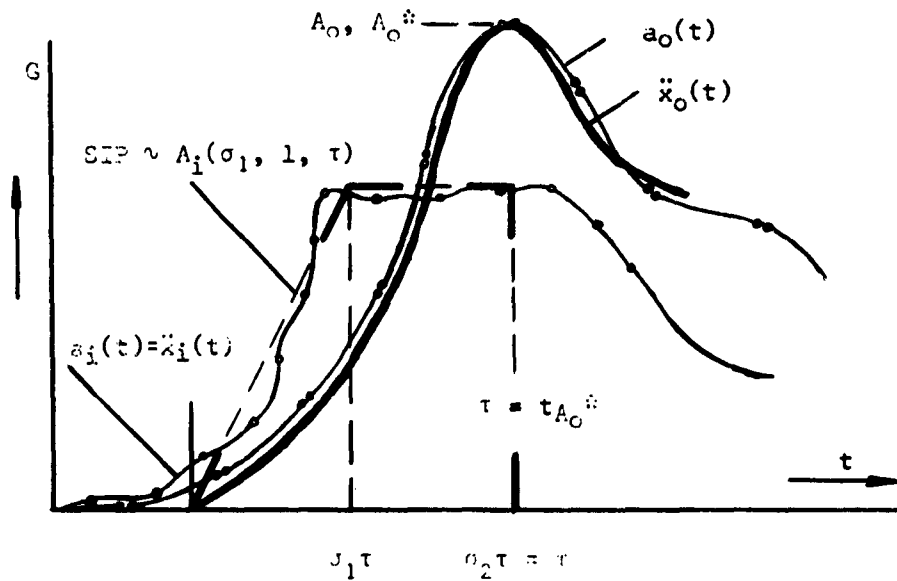
Figure 15   Impact Profile Standardization

Most impact recordings are of irregular shape and not shown in the report. The "hand smoothed" impact profiles $a_i(t)$ in Figures 7 through 13 have been standarized as explained by Figure 15. The standardization is achieved by replacing the initial part of the recorded, but "hand smoothed" impact profile $a_i(t)$ by a standard impact profile $A_i(\sigma_1, \sigma_2, \tau)$. Only those replacements for $\sigma_2 = 1$ are described in this report. (In all other cases, $\sigma_2 \neq 1$, similar procedures can be applied.) The total impact pulse time τ of the

replacing standard impact profile $A_i(\sigma_1, 1, \tau)$ is identified by the time $t_{A_O}^*$ at which the response peak A_O^* resulting from the trial and error computer approximation $\ddot{x}_O(t) \rightarrow a_O(t)$ by use of the "hand smoothed" impact (input) profile $a_i(t) = \ddot{x}_i(t)$ is found.

The impact peak level A_i is the same for all profiles, original $a_i(t)$ or standardized $A_i(\sigma_1, 1, \tau)$.

2. Physical Model Response (Appendix)

The computer data of the second-order spring-mass system (Section IIa) excited by standard impact profiles have been plotted in Figures 16, 17 and 18. Response peak level and rise time are represented by the symbols A and t_A with the subscripts i, o1, o2, o3, identifying input, output, first, second, and third peak respectively.

Figure 16, restricted to $\zeta = 0$, illustrates that clear dependencies exist for impact durations up to $\tau = T/2$. In the range $\tau = T/2$ to $2T$ the applied plotting of only three points proves to be insufficient for use of interpolation. Additional measurements would be necessary to clarify this area.

Figures 17 and 18 apply a particular plotting insofar as the rise time $t_{A_{O1}}$ of the response peak A_{O_1} is used as a reference parameter.

IV

ACCURACY OF PROCEDURES

a. Human Testing

A comparison between the sled entrance velocity and the measured impact history $v_{(entrance)} \sim \int a_i dt_{(impact)}$ is the only means of relative accuracy survey since no direct accuracy controls of velocity or acceleration were available. The entrance velocity was measured by use of break wires (Berkley counters); the integration of the complete acceleration-time tracks of the original records (as far as available) was achieved by use of a planimeter, including all shock type oscillations inherent in these recordings. The data are given in Table II.
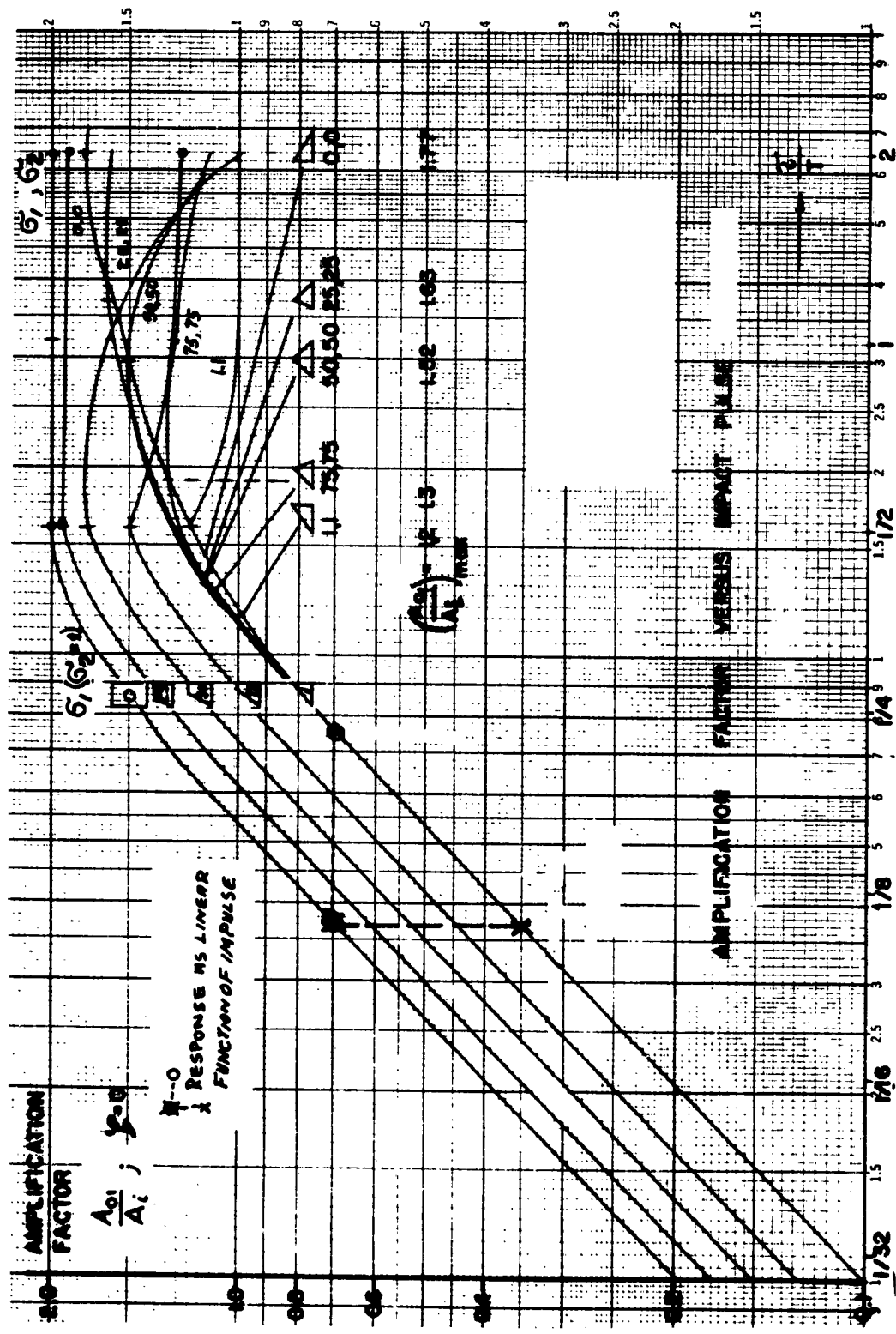
Figure 16   Amplification Factor Versus Impact Pulse
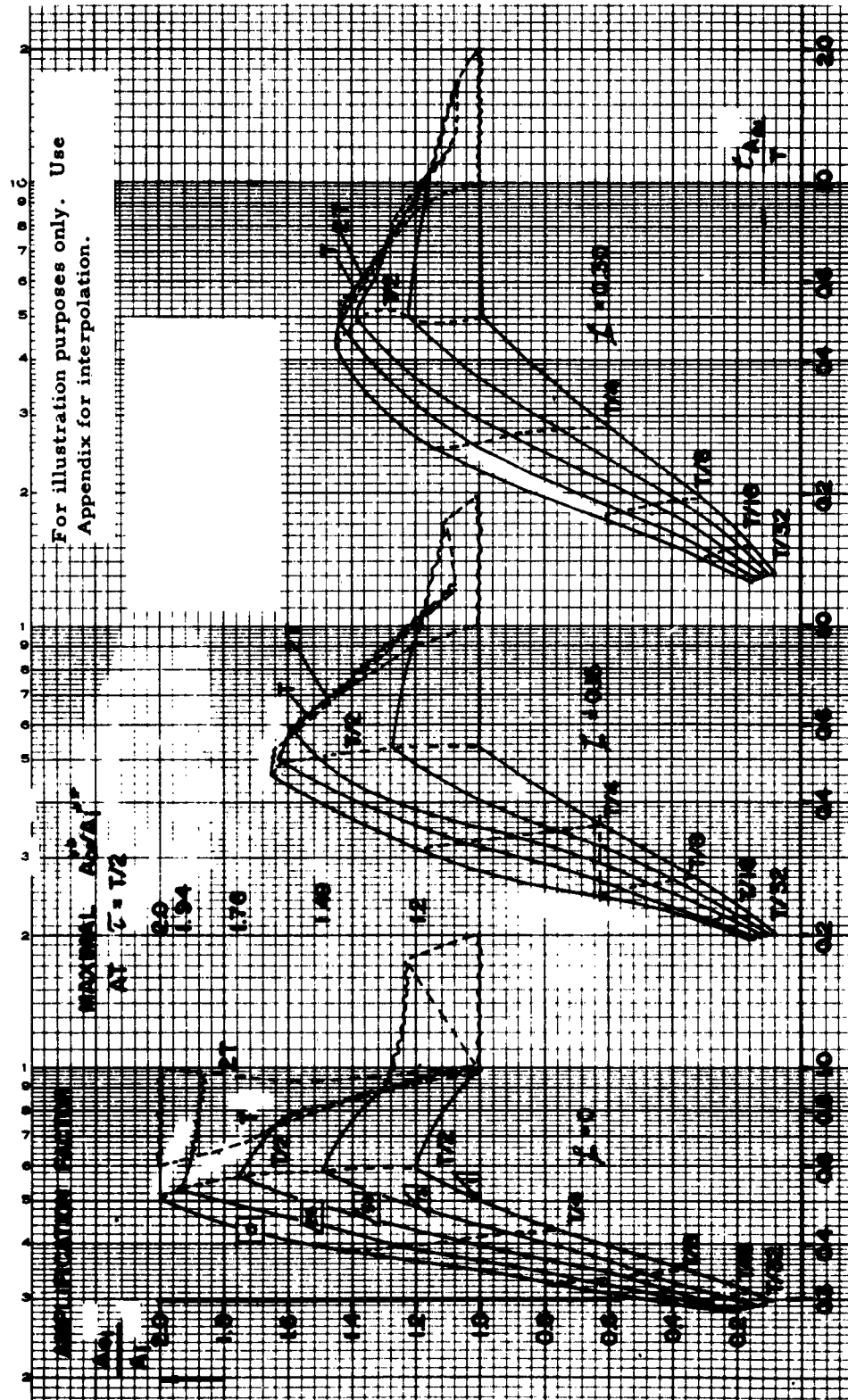
Figure 17   Amplification Factor Versus Response Peak Rise Time
(Trapezoidal Impact Profiles)

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Figure 18   Amplification Factor Versus Response Peak Rise Time
(Triangular Impact Profiles)
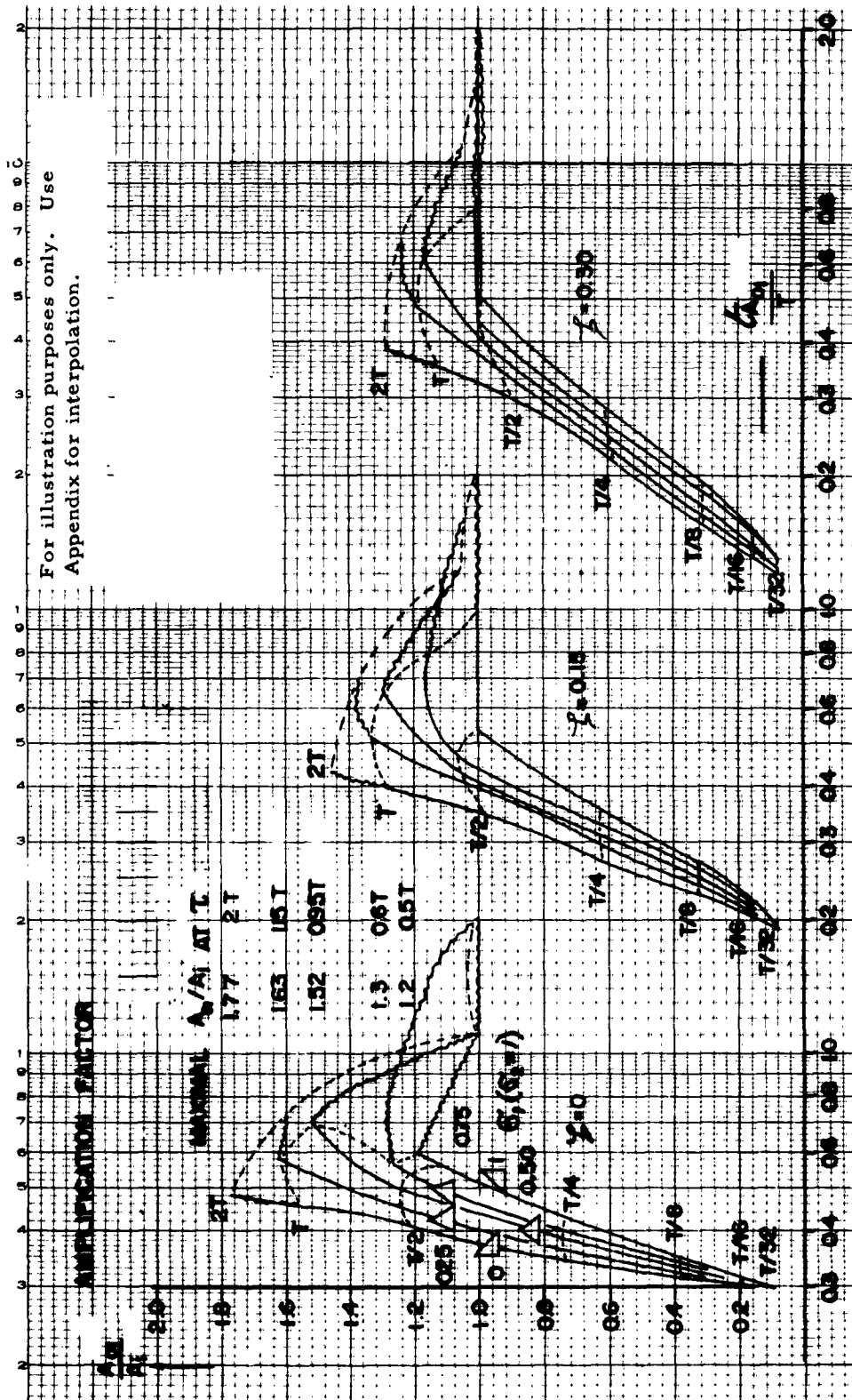
Table II Accuracy of Recordings

	Entrance Velocity ft/sec	
Test No.	v (Breakwire)	$\int a_i dt$ (Planimeter)
335	48.1	44.6
319	47.4	4?.5
612	44.4	40.0
842	40.3	41.6
790	40.4	39.7
846	39.7	40.0
798	49.2	47.0
756	57.8	65.5
847	43.6	42.8

b. Standardization of Impact Profile

Both "hand smoothing" of the original tracks and standardization $A_i(\sigma_1, 1, \tau)$ of the "hand smoothed" profiles $a_i(t)$ presented in this report were achieved manually. This manipulation can be only vaguely described as a procedure of averaging at the discretion of the evaluator. With reference to the rise time $t_{A_{o1}}$ of the first response peak A_{o1} resulting from the standard profile $A_i(\sigma_1, 1, \tau)$, the original tracks, the "hand smoothed" profiles $a_i(t)$ and the standardized profiles $A_i(\sigma_1, 1, \tau)$ were integrated by use of a planimeter and are reported in Table III.

Table III Accuracy of Profile Modification

	$\int a_i dt$ (ft/sec)		
Test No.	Original track	Hand smoothed profile $a_i(t)$	Standardized profile $A_i(\sigma_1, 1, \tau)$
319	15.9	13.6	13.6
335	27.4	21.5	---
612	9.3	11.5	11.0
756	13.8	14.1	14.6
790	11.5	11.9	12.5
798	19.1	19.5	20.4
842	26.1	15.5	15.3
844	15.1	15.5	15.1
846	16.5	17.4	17.8

c. Response Comparison

A comparison of the response peak levels and their rise times of the test records (A_o, t_{A_o}) and of the spring-mass model applied with the recorded impact profile $a_i(t)$ by use of trial and error approximation (A_o^*, $t_{A_o}^*$) and with the standard impact profile (A_{o1}, $t_{A_{o1}}$) is given in Table IV.

Whenever A_{o1}/A_i could be found by interpolation of Figures 17 and 18, this amplification factor was used to determine the response peak A_{o1}. Otherwise, the factor A_{o1}/A_i was computed by use of A_o^*/A_i. Similarly, the response peak rise time $t_{A_{o1}}$ was found by interpolation or by use of $t_{A_o}^*/T$.

Of course, the experimental data from Figures 7 through 13 with reference to the standardized profile are identical with the data gained from the physical model based on standard impact profiles of Figures 17 and 18 if identical values of ω_n and ζ_i are applied. Consequently, a comparison between the recorded and the model data cannot be considered as a criterion of response predictability, but merely as a criterion of accuracy of evaluation procedures if recorded impact profiles are replaced by standardized impact profiles. In this regard it is found that the response peaks A_o, A_{o1}^*, A_{o1} and the respective rise times t_{A_o}, and $t_{A_{o1}}^*$ and $t_{A_{o1}}$ are in good accord.

V

RESULTS

One must be aware that the human impact tests used were designed to serve other purposes than those pursued in this study. Therefore, the results of this investigation must be presented with all reservations which might accrue from the view of adequacy of test conditions or validity of recordings or data reduction. In spite of this restriction, it was shown that:

a. The dynamic response of the chest (accelerometer) of the seated human subjected to $+G_x$ impact can be approximated by a second or higher order system. However, the necessary trial and error variation of natural frequency ω_n^* and damping ζ^* during one and the same run prevent the use of (linear) spring-mass systems to predict the dynamic response of the chest (accelerometer) unless the inconsistencies in ω_n^* and ζ^* can be eliminated by refinement of test preparation or lawful recognition of their physical or physiological mechanics.

Table IV   Comparison of Dynamic Response Data

Subject Number	Test Number	A_i (σ_i (σ_i, σ_a, T))	PHYSICAL PROPERTIES: Natural Frequency ω_n RAD/SEC	τ SEC	Initial Damping ζ_i	AMPLIFICATION FACTOR By interpolation in $\sigma_i, \sigma_a, \tau, \zeta$ (not shown) $\frac{A_o}{A_i}$	RESPONSE PEAK "G" SIP A_{o_1}	APPROX A_o^*	RECORDED A_o	PULSE (τ/T)	RISE TIME SIP t_{o_1}	APPROX t_o^*	RECORDED σ_{SIP}	σ_R	Notes
I	318	26 (-, -, -)	140	0.045	0			43	63/43						Old Test Set Up
	335	40 (-, -, -)	150	0.035	0			62	86/76						Old Test Set Up
	549	14 (0.24, 1.0, 0.562T)	130	0.04	0.2	1.51	21.2	21.5	21.5	0.48	0.023	0.027	0.027	0.042	New Test Set Up
II	319	25.5 (0.72, 1.0, 0.69T)	163	0.0365	0.65	1.50	22.5	36	36	0.69	+0.021	0.0265	0.031	0.036	Old Test Set Up Erratic Response
	612	25 (0.18, 1.0, 0.58T)	145/150	0.0433	0.25	1.50		23.5	23.5	0.48	+0.021	0.025	0.025	0.045	New Test Set Up
	842	20 (0.67, 1.0, 0.77T)	134/146	0.047	0.375	1.55		31	31	0.77	+0.031	0.036	0.040	0.055	New Test Set Up
III	380	23.5 (0.245, 0.245, 2T)	140	0.045	0	1.63	23.5	40	43	0.70	+0.0035	0.0325	0.0325	0.0325	Old Test Set Up
	607	14 (0.175, 1.0, 0.55T)	120/121	0.052	0.06	1.0	25.2	25	25	0.52	+0.027	0.0255	0.0255	0.046	New Test Set Up
	755	20.5 (0.48, 1.0, 0.59T)	110/114	0.057	0.25	1.40	29.5	30	29.5	0.54	+0.031	0.0335	0.035	0.04	New Test Set Up
IV	332	36.5 (0.30, 0.30, 2T)	150	0.042	0	1.49	54	52.5	54	0.42	+0.0345	0.0315	0.0315	0.0405	Old Test Set Up
	598	15 (0.34, 1.0, 0.57T)	120	0.052	0.2	1.51	22.6	22	22	0.50	+0.026	0.0295	0.0275	0.045	New Test Set Up
V	606	16 (0.24, 1.0, 0.66T)	150	0.042	0.15	1.61	25.7	27	27.5	0.52	+0.022	0.0275	0.0275	0.046	New Test Set Up
	790	10.5 (0.5, 1.0, 0.72T)	100	0.063	0	1.2	19	16	16	0.65	+0.041	0.045	0.035	0.0535	New Test Set Up With Chest Parachute
VI	751	19 (0.9, 1.0, 1.2T)	130	0.048	0.15	1.10		21	22	1.20		0.0575	0.0575	0.055	New Test Set Up
	846	19 (0.6, 1.0, 0.8T)	120	0.052	0	1.60		34	33	0.50		0.0415	0.0405	0.0515	New Test Set Up
	798	23.5 (0.63, 1.0, 0.9T)	120	0.052	0.3	1.16		27	27	0.90		0.0475	0.0475	0.055	New Test Set Up with Chest Parachute
VII	756	21.5 (0.51, 1.0, 0.5T)	110/127	0.057	0.5	1.30	26	27.5	27.5	0.49	+0.026	0.0265	0.031	0.036	New Test Set Up
	844	20 (0.62, 1.0, 0.73T)	130/132	0.048	0.15	1.50		30	29	0.73		0.035	0.035	0.0575	New Test Set Up

Note (Subject I): No reasonable approximation possible for any value of ω_n $\zeta = 0$. Only lower response recording of 435 could be approximated.

$\frac{A_o}{A_i}$ $\longrightarrow$ found by interpolation in $\sigma_i, \sigma_a, \tau, \zeta$ (not shown in report) $\longrightarrow$ found by A_o^* / A_i

$\frac{T}{\tau}$ $\longrightarrow$ found by interpolation in $\sigma_i, \sigma_a, \tau, \zeta$ (not shown in report) $\longrightarrow$ found by $t_{A_o}^* / T$

σ_R Coordinate origin of recorded impact profile. O_{SIP} coordinate origin of standardized impact profile

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b. The complete response coverage shown in Figures 4, 5, and 6 has proven to be an excellent means to illustrate the continuous dynamic response of the chest (accelerometer). The trial and error approximation of the complete response history established that:

1. The damping coefficient experiences a drastic change at the time of chest (accelerometer) response peak or shortly thereafter.

2. The variation of the damping coefficient ζ^* spreading over a range from $\zeta^* = 0$ to $\zeta^* = 1$ seemed to be more effective than the variation of the natural frequency ω_n^*.

3. A one second-order system was sufficient in most cases to approximate the first peak level and rise time of the dynamic chest (accelerometer) response.

c. The limited response coverages (Fig. 7 through 13) using a second-order spring-mass system can be simplified by applying standardized impact profiles. Though starting out with a different damping coefficient for different and same test subjects, the initial value of the damping coefficient ζ_i^* was never required to be varied before the first chest (accelerometer) response peak was reached.

At first glance at the plotting of ω_n^* versus impact peak "G" in Figure 19, it seems that the natural frequency increases with increasing impact peak "G". However, knowing that the chest instrumentation was changed for all tests subsequent to test No. 359, a confrontation of the "No. 300" test series and all subsequent tests might be misleading.

All tests subsequent to the "No. 300" test series show a difference of 40 rad/sec between the lowest and highest value of ω_n^*. However, for one and the same test subject this difference varies from 10 to 20 rad/sec only, if the two measurements available for each subject can be considered sufficient to make this distinction.

Figure 19 illustrates the wide variation of the initial damping coefficient ζ_i^* with reference to the response-time history limited by the response-peak onset time.

d. It should be realized that the onset rate A_i/t_{A_i} of the impact peak is not recognizable as a parameter of autonomous significance for the investigated pulse durations up to 2T (Fig. 16). If the investigator wants to consider the time element of physiological effects of impact of this duration range, it is more adequate to use the rise time of the dynamic response peak A_0 since the physiological changes of impact very likely result from the change of the physical state of the body.
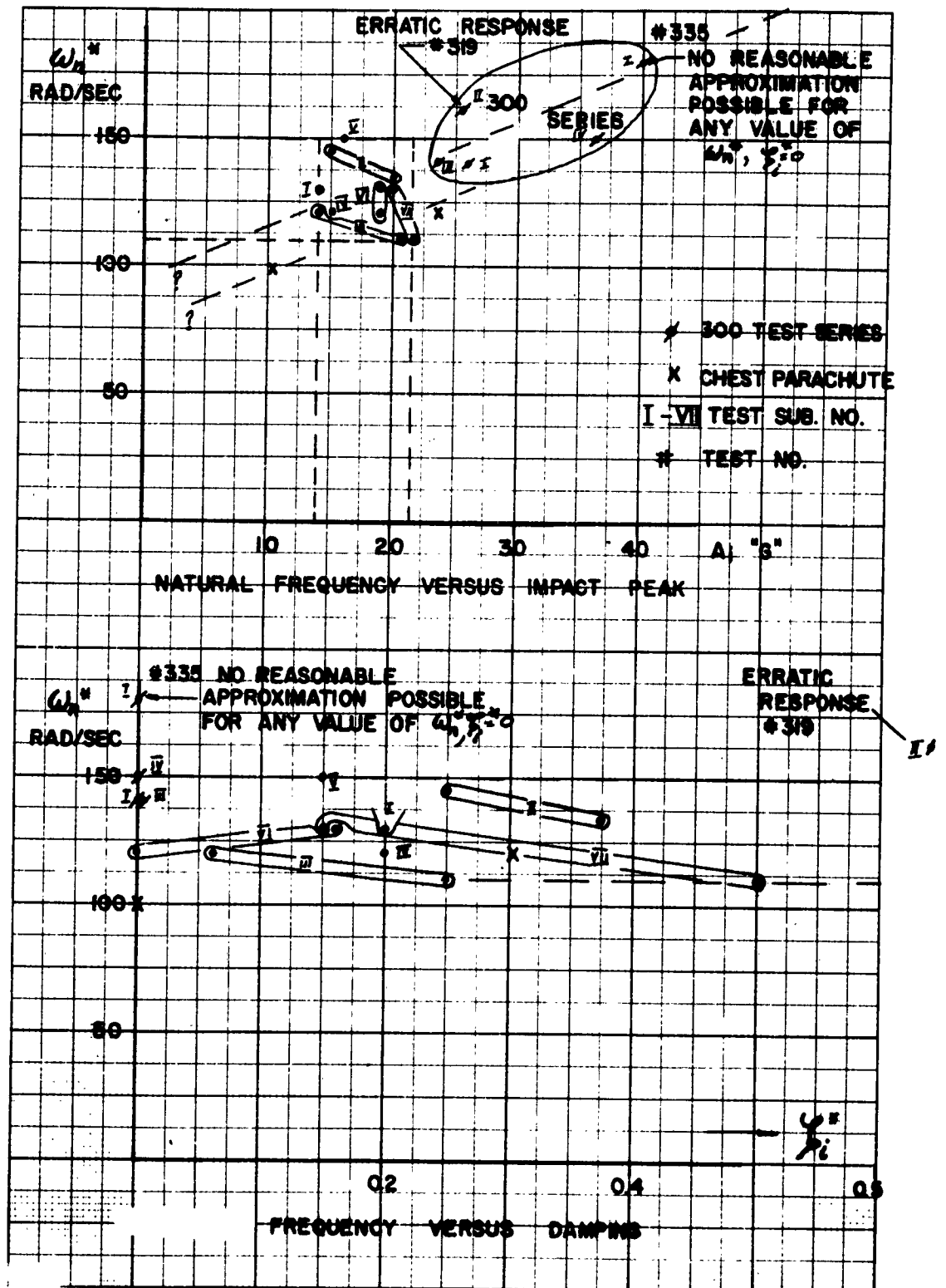
Figure 19   Dynamic Characteristic (ω_n ζ) of Humans Subjected
to +G_x Impact

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There is evidence that impact profiles of short enough duration
will permit the development of free vibration subsequent to the
transfer dynamics. The damping characteristic of the free vibration
can provide for a comparison between the natural frequency of the
undamped system, as established in this report, with the resonance
frequency of steady state vibration as an additional means to vali-
date the model concept chosen.

From the view of utilization of the described response analysis,
it could aid the biodynamic investigator to learn by measuring at
various locations, the response distribution on humans (externally)
and animals (externally and internally). The simultaneous measure-
ments at different locations would also be helpful to validate the
applied evaluation procedures.

The internal instrumentation of animals can open an interesting
field of simplified and informative research if the assumption of
response predictability applies. Since, in this case, the momentary
stress level of the body components depends directly on the dynamic
behavior of the body, the inappropriate accelerometers (three compo-
nents, heavy, bulky) can be replaced by absolute pressure transducers
which would furnish information about the pressure history and the
dynamic characteristics (ω_n^*, ζ^*) as well. In combination with the
cineradiographic investigation of internal organ displacements men-
tioned in the introduction a well rounded test program of organ stress
and strain during impact can be anticipated.

VI

RECOMMENDATIONS

It is recommended that additional investigations be made to validate
and utilize the described trial and error approximation of the dynamic
response of humans or animals subjected to impact.

From the view of validation of the assumption of the predictability
of the dynamic response of the body as a whole, study continuation
should concentrate on the means to improve the consistency of the
model characteristics ω_n^* and ζ_i^* with reference to variable impact
profiles. The results of this study indicate two main areas which
deserve closer attention. First, the drastic change of the damping
coefficient occurs at the time of the first response peak or shortly
thereafter. This evidence could be related directly with the direc-
tional change of the displacement of the chest wall and consequently
with the filling status of the lungs. In reverse, the difference of
the filling status of the lungs at the time of impact could also explain
the finding that the initial damping coefficient ζ_i^* for the same test
subject varies from test to test. A rigid control of the timing of

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impact with relation to the respiratory phases could benefit the medical investigator looking at the mechanics of the physiological and pathological alterations as well as the test engineer interested in controlling the independent variables. The second area of interest is the wide spread of the natural frequency ω_n* of the same and of different test subjects. These differences, at least in part, could result from the mounting of the accelerometer pad to the restraint belt which was not particularily contolled in terms of restraining force and displacement. In summary, the following recommendations are made:

a. Provide for rigid controls of respiratory function during impact in terms of timing and filling grade.

b. Secure rigid controls of the effect of the restraint systems upon the accelerometer.

c. Mount accelerometers at different, external locations (humans).

d. Use pressure transducers for internal instrumentation of animals.

e. Restrict additional program initiation to total impact duration of $\tau < 0.5T$ to avoid the range of response overlap (Fig. 17) and to determine the characteristics of the resulting damped free vibration.

APPENDIX

ANALOG COMPUTER RESPONSE OF SECOND ORDER MODEL TO STANDARD IMPACT PROFILES

In the main body of this report the analog computer has been used to simulate the elastic behavior of the human body. The same computer setup was used for a parametric study of the second-order spring-mass system of the equation (2) on page 5.

The variables of the parametric evaluation are listed in Table V. The measurements are listed in Table VI.

The output measurements A_{o1}, A_{o2}, and A_{o3} in volts are based on an input of 20 volts. Some continuous response modes are illustrated in Figures 20, 21 and 22.

Table V   Symbol Chart

Table V   Symbol Chart
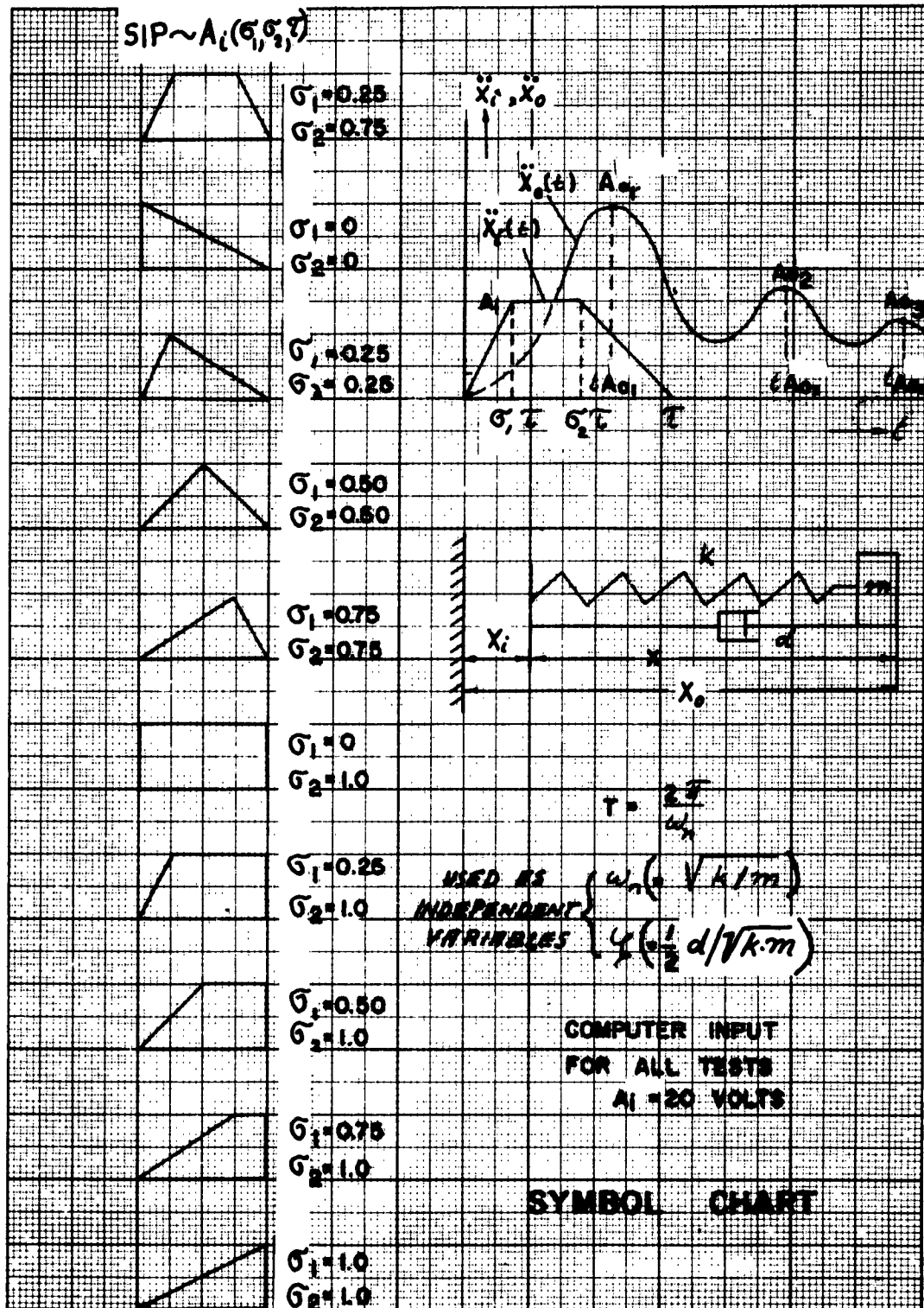
Table VI Computer Response Data of SIP

σ_1	σ_2	τ	Damp Coeff. ζ	First response peak A_{o1}	time $t_{A_{o1}}$	Second response peak A_{o2}	Third response peak A_{o3}
0.25	0.75	2T	0	32.90	0.752T'	30.11	25.91
0	0	2T	0	35.44	0.481T	25.18	20.36
0.25	0.25	2T	0	32.01	0.731T	18.34	17.19
0.5	0.5	2T	0	20.02	1.103T	0	0
0.75	0.75	2T	0	22.47	1.639T	17.21	17.17
0	1	2T	0	39.94	0.506T	39.92	0
0.25	1.0	2T	0	37.76	0.756T	32.75	23.17
0.5	1	2T	0	19.95	0.988T	19.92	19.92
0.75	I	2T	0	24.07	1.771T	20.21	20.21
1	1	2T	0	19.88	1.998T	19.85	19.85
0.25	0.75	T	0	38.00	0.629T	25.38	25.36
0	0	T	0	31.17	0.450T	20.23	20.23
0.25	0.25	T	0	32.51	0.575T	24.26	24.26
0.5	0.5	T	0	30.31	0.701T	25.62	25.62
0.75	0.75	T	0	25.51	0.838T	24.03	24.03
0	1	T	0	39.95	0.506T	0	0
0.25	1	T	0	38.00	0.630T	14.53	14.53
0.5	1	T	0	32.72	0.757T	23.62	23.62
0.75	1	T	0	25.95	0.892T	24.57	24.57
1	1	T	0	20.20	1.000T	20.00	20.00
0.25	0.75	T/2	0	36.03	0.503T	36.01	36.01
0	0	T/2	0	24.01	0.409T	24.78	24.78
0.25	0.25	T/2	0	25.24	0.458T	25.18	25.18
0.5	0.5	T/2	0	25.72	0.505T	25.70	25.70
0.75	0.75	T/2	0	25.08	0.505T	25.06	25.06
0	1	T/2	0	39.96	0.503T	39.96	39.96
0.25	1	T/2	0	38.72	0.533T	38.69	38.69
0.5	1	T/2	0	35.14	0.562T	35.11	35.11
0.75	1	T/2	0	29.84	0.584T	29.81	29.81
1	1	T/2	0	23.82	0.594T	23.80	23.80
0.25	0.75	T/4	0	22.08	0.381T	22.06	22.06
0	0	T/4	0	14.68	0.343T	14.67	14.67
0.25	0.25	T/4	0	14.94	0.364T	14.93	14.93
0.5	0.5	T/4	0	15.03	0.384T	15.01	15.01
0.75	0.75	T/4	0	14.88	0.405T	14.87	14.87
0	1	T/4	0	28.24	0.380T	28.22	28.22
0.25	1	T/4	0	25.31	0.396T	25.29	25.29
0.5	1	T/4	0	21.97	0.409T	21.95	21.95
0.75	1	T/4	0	18.39	0.421T	18.38	18.38
1	1	T/4	0	14.74	0.427T	14.75	14.75

(Table VI Cont'd)

σ_1	Profile σ_2	τ	Damp Coeff. ζ	First response peak A_{o_1}	response time $t_{A_{o_1}}$	Second response peak A_{o2}	Third response peak A_{o3}
0.25	0.75	T/8	0	11.55	0.325T	11.55	11.55
0	0	T/8	0	7.68	0.311T	7.68	7.68
0.25	0.25	T/8	0	7.75	0.321T	7.75	7.75
0.5	0.5	T/8	0	7.77	0.331T	7.77	7.77
0.75	0.75	T/8	0	7.74	0.342T	7.74	7.74
0	1	T/8	0	15.26	0.323T	15.26	15.26
0.25	1	T/8	0	13.45	0.331T	13.45	13.45
0.5	1	T/8	0	11.57	0.340T	11.57	11.57
0.75	1	T/8	0	9.66	0.346T	9.66	9.66
1	1	T/8	0	7.75	0.352T	7.75	7.75
0.25	0.75	T/16	0	5.80	0.306T	5.80	5.80
0	0	T/16	0	3.81	0.308T	3.81	3.81
0.25	0.25	T/16	0	3.84	0.313T	3.84	3.84
0.5	0.5	T/16	0	3.93	0.300T	3.93	3.93
0.75	0.75	T/16	0	3.92	0.303T	3.92	3.92
0	1	T/16	0	7.81	0.291T	7.81	7.81
0.25	1	T/16	0	6.86	0.295T	6.86	6.86
0.5	1	T/16	0	5.89	0.300T	5.89	5.89
0.75	1	T/16	0	4.93	0.304T	4.93	4.93
1	1	T/16	0	3.96	0.308T	3.96	3.96
0.25	0.75	T/32	0	2.92	0.288T	2.92	2.92
0	0	T/32	0	1.92	0.294T	1.92	1.92
0.25	0.25	T/32	0	1.94	0.296T	1.94	1.94
0.5	0.5	T/32	0	1.94	0.299T	1.94	1.94
0.75	0.75	T/32	0	1.94	0.301T	1.94	1.94
0	1	T/32	0	3.97	0.283T	3.97	3.97
0.25	1	T/32	0	3.51	0.287T	3.51	3.51
0.5	1	T/32	0	3.00	0.289T	3.00	3.00
0.75	1	T/32	0	2.51	0.293T	2.51	2.51
1	1	T/32	0	2.02	0.299T	2.02	2.02

(Table VI Cont'd)

σ_1	Profile σ_2	τ	Damp Coeff. ζ	First response peak A_{o1}	response time $t_{A_{o1}}$	Second response peak A_{o2}	Third response peak A_{o3}
0.25	0.75	2T	0.15	28.36	0.731T	21.44	6.44
0	0	2T	0.15	29.15	0.430T	10.77	2.02
0.25	0.25	2T	0.15	27.40	0.700T	7.86	2.52
0.5	0.5	2T	0.15	20.98	1.250T	0.49	0.10
0.75	0.75	2T	0.15	20.83	1.589T	6.01	2.30
0	1	2T	0.15	32.96	0.462T	24.97	6.88
0.25	1	2T	0.15	28.35	0.732T	23.19	8.50
0.5	1	2T	0.15	21.56	1.245T	7.97	3.05
0.75	1	2T	0.15	22.05	1.744T	8.30	3.18
1	1	2T	0.15	19.93	1.981T	7.94	3.07
0.25	0.75	T	0.15	31.72	0.585T	8.86	3.42
0	0	T	0.15	25.63	0.398T	5.06	1.96
0.25	0.25	T	0.15	26.75	0.518T	7.10	2.75
0.5	0.5	T	0.15	25.81	0.645T	8.45	3.27
0.75	0.75	T	0.15	23.11	0.811T	8.77	3.38
0	1	T	0.15	32.98	0.458T	5.00	1.94
0.25	1	T	0.15	31.72	0.585T	6.91	2.68
0.5	1	T	0.15	28.35	0.728T	9.35	3.62
0.75	1	T	0.15	24.21	0.902T	9.64	3.73
1	1	T	0.15	20.09	0.993T	7.94	3.06
0.25	0.75	T/2	0.15	30.18	0.450T	11.74	4.52
0	0	T/2	0.15	19.87	0.347T	7.65	2.95
0.25	0.25	T/2	0.15	20.75	0.396T	8.05	3.11
0.5	0.5	T/2	0.15	21.37	0.444T	8.29	3.20
0.75	0.75	T/2	0.15	21.35	0.489T	8.23	3.18
0	1	T/2	0.15	32.96	0.459T	13.07	5.05
0.25	1	T/2	0.15	32.50	0.499T	12.67	4.88
0.5	1	T/2	0.15	29.94	0.503T	11.54	4.45
0.75	1	T/2	0.15	25.53	0.524T	9.83	3.80
1	1	T/2	0.15	20.41	0.534T	7.87	3.04
0.25	0.75	T/4	0.15	18.65	0.311T	7.19	2.77
0	0	T/4	0.15	12.38	0.270T	4.78	1.83
0.25	0.25	T/4	0.15	12.45	0.289T	4.80	1.85
0.5	0.5	T/4	0.15	12.59	0.311T	4.85	1.87
0.75	0.75	T/4	0.15	12.62	0.333T	4.86	1.88
0	1	T/4	0.15	23.85	0.313T	9.19	3.56
0.25	1	T/4	0.15	21.38	0.327T	8.24	3.18
0.5	1	T/4	0.15	18.58	0.340T	7.14	2.77
0.75	1	T/4	0.15	15.58	0.350T	6.02	2.32
1	1	T/4	0.15	12.49	0.354T	4.82	1.85

(Table VI Cont'd)

σ_1	Profile σ_2	τ	Damp Coeff. ζ	First response peak A_{o1}	response time $t_{A_{o1}}$	Second response peak A_{o2}	Third response peak A_{o3}
0.25	0.75	T/8	0.15	9.79	0.248T	3.78	1.44
0	0	T/8	0.15	6.53	0.230T	2.52	0.95
0.25	0.25	T/8	0.15	6.49	0.240T	2.50	0.94
0.5	0.5	T/8	0.15	6.54	0.250T	2.53	0.95
0.75	0.75	T/8	0.15	6.58	0.261T	2.53	0.95
0	1	T/8	0.15	12.91	0.249T	4.98	1.93
0.25	1	T/8	0.15	11.38	0.256T	4.40	1.70
0.5	1	T/8	0.15	9.80	0.263T	3.80	1.47
0.75	1	T/8	0.15	8.19	0.269T	3.17	1.24
1	1	T/8	0.15	6.58	0.272T	2.55	0.98
0.25	0.75	T/16	0.15	4.92	0.214T	1.90	0.73
0	0	T/16	0.15	3.28	0.204T	1.26	0.49
0.25	0.25	T/16	0.15	3.25	0.209T	1.25	0.48
0.5	0.5	T/16	0.15	3.27	0.214T	1.26	0.49
0.75	0.75	T/16	0.15	3.31	0.218T	1.27	0.49
0	1	T/16	0.15	6.51	0.213T	2.51	0.97
0.25	1	T/16	0.15	5.71	0.217T	2.20	0.85
0.5	1	T/16	0.15	4.90	0.220T	1.89	0.73
0.75	1	T/16	0.15	4.08	0.222T	1.58	0.61
1	1	T/16	0.15	3.27	0.221T	1.26	0.49
0.25	0.75	T/32	0.15	2.47	0.196T	0.95	0.37
0	0	T/32	0.15	1.65	0.191T	0.63	0.24
0.25	0.25	T/32	0.15	1.63	0.194T	0.63	0.24
0.5	0.5	T/32	0.15	1.64	0.197T	0.63	0.24
0.75	0.75	T/32	0.15	1.65	0.199T	0.64	0.25
0	1	T/32	0.15	3.22	0.196T	1.24	0.48
0.25	1	T/32	0.15	2.78	0.198T	1.07	0.42
0.5	1	T/32	0.15	2.41	0.200T	0.93	0.36
0.75	1	T/32	0.15	2.00	0.200T	0.77	0.30
1	1	T/32	0.15	1.59	0.202T	0.60	0.23

σ_1	Profile σ_2	τ	Damp Coeff. ζ	First response peak A_{01}	response time $t_{A_{0i}}$	Second response peak A_{02}	Third response peak A_{03}
0.25	0.75	2T	0.30	25.91	0.714T	19.80	2.31
0	0	2T	0.30	25.71	0.385T	7.57	0.48
0.25	0.25	2T	0.30	24.77	0.668T	0.66	0.10
0.5	0.5	2T	0.30	21.08	1.087T	0.62	0.10
0.75	0.75	2T	0.30	20.45	1.549T	2.41	0.35
0	1	2T	0.30	29.00	0.423T	21.24	3.32
0.25	1	2T	0.30	25.91	0.711T	20.81	3.45
0.5	1	2T	0.30	21.88	1.188T	19.76	3.32
0.75	1	2T	0.30	21.50	1.700T	3.48	0.50
1	1	2T	0.30	19.90	1.983T	3.23	0.47
0.25	0.75	T	0.30	28.12	0.544T	3.51	0.50
0	0	T	0.30	22.64	0.351T	1.41	0.21
0.25	0.25	T	0.30	23.79	0.475T	2.31	0.33
0.5	0.5	T	0.30	23.43	0.622T	3.01	0.43
0	1	T	0.30	29.00	0.422T	16.68	2.94
0.75	0.75	T	0.30	21.85	0.798T	3.33	0.47
0.25	1	T	0.30	28.12	0.554T	3.31	0.48
0.5	1	T	0.30	25.88	0.712T	3.83	0.55
0.75	1	T	0.30	23.33	0.915T	3.82	0.55
1	1	T	0.30	20.11	0.993T	3.16	0.46
0.25	0.75	T/2	0.30	27.32	0.414T	4.08	0.57
0	0	T/2	0.30	17.85	0.295T	2.63	0.38
0.25	0.25	T/2	0.30	18.76	0.345T	2.78	0.40
0.5	0.5	T/2	0.30	19.53	0.398T	2.88	0.41
0.75	0.75	T/2	0.30	19.88	0.452T	2.88	0.41
0	1	T/2	0.30	29.00	0.421T	4.60	0.66
0.25	1	T/2	0.30	28.77	0.484T	4.43	0.64
0.5	1	T/2	0.30	27.47	0.498T	4.05	0.58
0.75	1	T/2	0.30	24.26	0.498T	3.46	0.50
1	1	T/2	0.30	19.68	0.498T	2.78	0.40
0.25	0.75	T/4	0.30	17.97	0.246T	2.50	0.36
0	0	T/4	0.30	11.70	0.2171T	1.66	0.24
0.25	0.25	T/4	0.30	11.90	0.231T	1.67	0.24
0.5	0.5	T/4	0.30	12.12	0.244T	1.69	0.25
0.75	0.75	T/4	0.30	12.16	0.261T	1.79	0.25
0	1	T/4	0.30	22.97	0.251T	3.20	0.46
0.25	1	T/4	0.30	20.61	0.257T	2.87	0.42
0.5	1	T/4	0.30	17.94	0.269T	2.50	0.37
0.75	1	T/4	0.30	15.03	0.278T	2.09	0.31
1	1	T/4	0.30	12.04	0.283T	1.68	0.25

(Table VI Cont'd)

| σ_1	Profile σ_2	τ	Damp Coeff. ζ	First response peak A_{o1}	response time $t_{A_{o1}}$	Second response peak A_{o2}	Third response peak A_{o3}
0.25	0.75	T/8	0.30	9.38	0.174T	1.29	0.18
0	0	T/8	0.30	6.24	0.153T	0.86	0.12
0.25	0.25	T/8	0.30	6.20	0.163T	0.85	0.12
0.5	0.5	T/8	0.30	6.25	0.173T	0.86	0.12
0.75	0.75	T/8	0.30	6.28	0.184T	0.86	0.12
0	1	T/8	0.30	12.39	0.175T	1.71	0.24
0.25	1	T/8	0.30	10.90	0.181T	1.51	0.21
0.5	1	T/8	0.30	9.38	0.188T	1.30	0.18
0.75	1	T/8	0.30	7.82	0.193T	1.08	0.15
1	1	T/8	0.30	6.27	0.195T	0.87	0.12
0.25	0.75	T/16	0.30	4.76	0.147T	0.66	0.09
0	0	T/16	0.30	3.16	0.131T	0.44	0.06
0.25	0.25	T/16	0.30	3.13	0.136T	0.43	0.06
0.5	0.5	T/16	0.30	3.16	0.141T	0.44	0.06
0.75	0.75	T/16	0.30	3.17	0.154T	0.44	0.06
0	1	T/16	0.30	6.30	0.142T	0.87	0.12
0.25	1	T/16	0.30	5.53	0.145T	0.77	0.11
0.5	1	T/16	0.30	4.74	0.149T	0.66	0.09
0.75	1	T/16	0.30	3.95	0.151T	0.55	0.08
1	1	T/16	0.30	3.15	0.153T	0.44	0.06
0.25	0.75	T/32	0.30	2.38	0.135T	0.331	0.05
0	0	T/32	0.30	1.59	0.121T	0.220	0.03
0.25	0.25	T/32	0.30	1.57	0.124T	0.218	0.03
0.5	0.5	T/32	0.30	1.58	0.126T	0.220	0.03
0.75	0.75	T/32	0.30	1.59	0.129T	0.221	0.03
0	1	T/32	0.30	3.11	0.126T	0.428	0.06
0.25	1	T/32	0.30	2.69	0.128T	0.374	0.06
0.5	1	T/32	0.30	2.29	0.129T	0.319	0.05
0.75	1	T/32	0.30	1.89	0.131T	0.264	0.04
1	1	T/32	0.30	1.50	0.131T	0.209	0.03
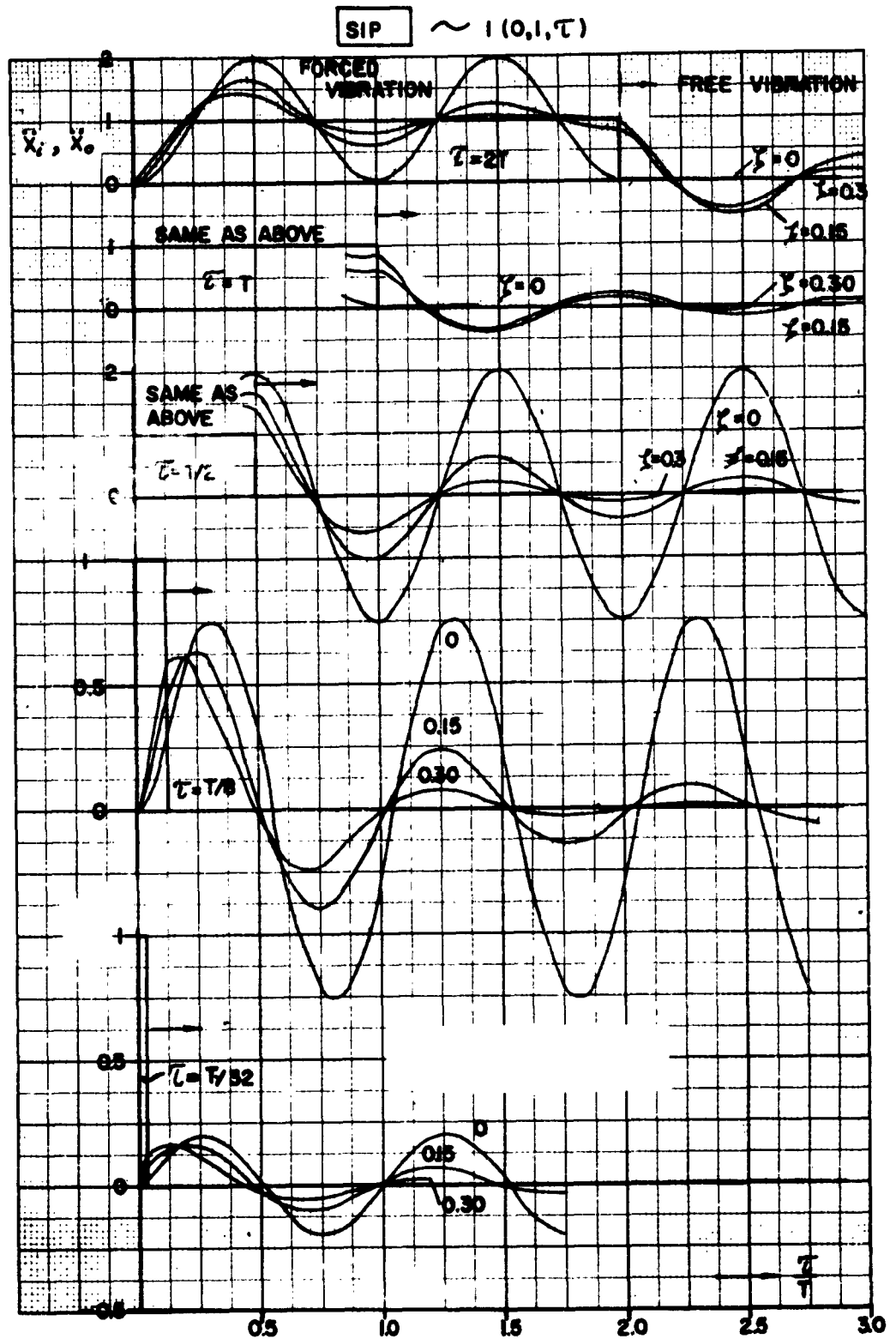
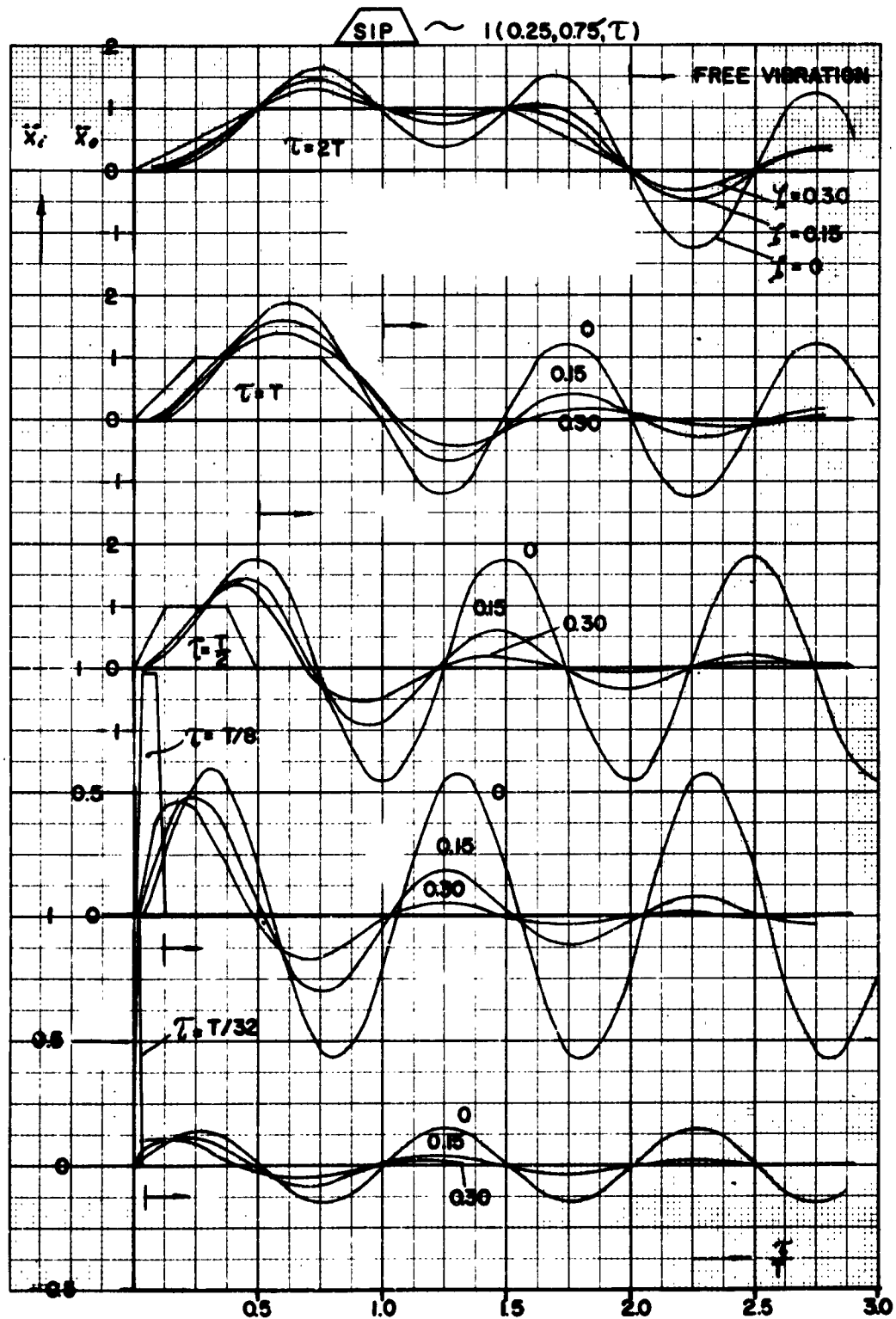Figure 20   Continuous Response Modes of SIP (Rectangular Profile)

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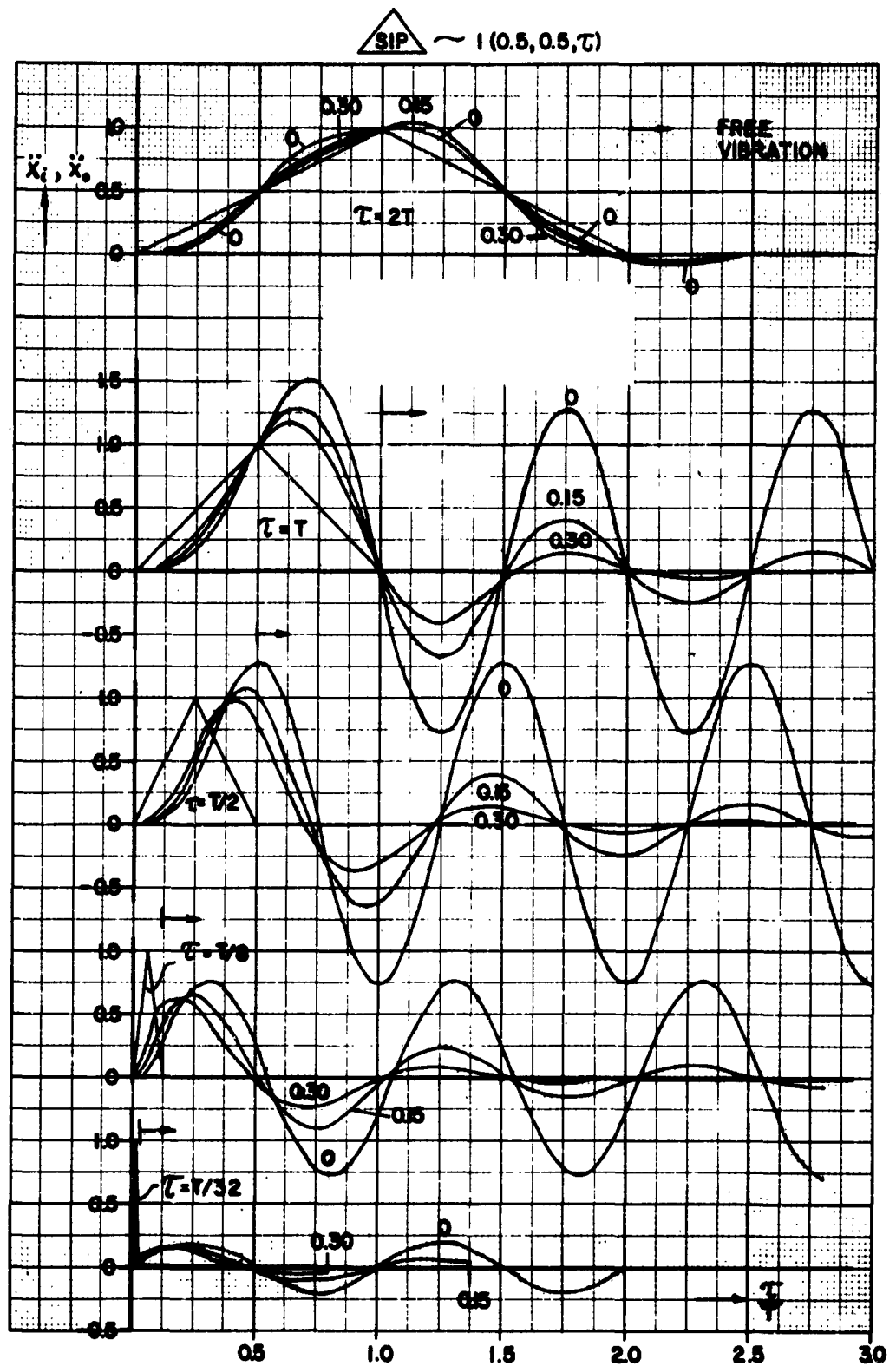Figure 21   Continuous Response Modes of SIP (Trapezoidal Profile)

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Figure 22   Continuous Response Modes of SIP (Triangular Profile)

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3 REPORT TITLE

DYNAMIC RESPONSE ANALYSIS OF $+G_x$ IMPACT ON MAN

4 DESCRIPTIVE NOTES (Type of report and inclusive dates)
Interim

5 AUTHOR(S) (Last name, first name, initial)
Feder, Hubert C. and Root, E. H.

6 REPORT DATE	7a TOTAL NO OF PAGES	7b NO OF REFS
November 1964	52	0

8a CONTRACT OR GRANT NO.	9a ORIGINATOR'S REPORT NUMBER(S)
b PROJECT NO 7231	ARL-TR-64-11
c Task 723106	9b OTHER REPORT NO(S) (Any other numbers that may be assigned this report)
d	

10 AVAILABILITY/LIMITATION NOTICES

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13 ABSTRACT

An analog computer was used to compare the dynamic response of an accelerometer placed over the sternum of human test subjects during impact in $+G_x$ direction with the response of second and higher order spring-mass systems. Identity of the response modes of both systems, human and mechanical, was approximated by trial and error modification of natural frequency and damping coefficient of the computer model used. With restriction to only a few cases investigated and to the particular test conditions, best compliance of complete response coverage is considered to result from the application of a single spring-mass system of irregularly varying damping coefficient. A parametric analysis of the single spring-mass system is presented to aid the use of standardized impact profiles. The usefulness of the method of response approximation has been established, but the validation of the underlying concept of response predictability needs further investigation.

DD FORM JAN 64 **1473**

14. KEY WORDS	LINK A		LINK B		LINK C	
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